

Efficient steady-state predictions of core plasma profiles with δf nonlinear gyrokinetics using the PORTALS framework

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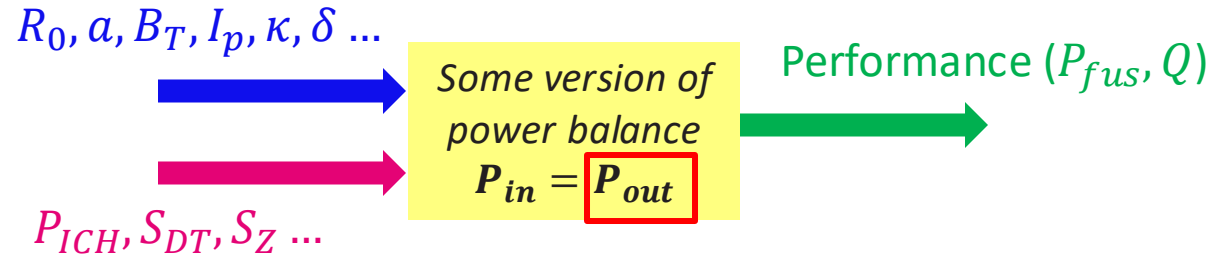
29th EU-US Transport Task Force Workshop

Budapest (Hungary), September 10th, 2025

This work was funded by US DOE DE-SC0024399 & Commonwealth Fusion Systems RPP020

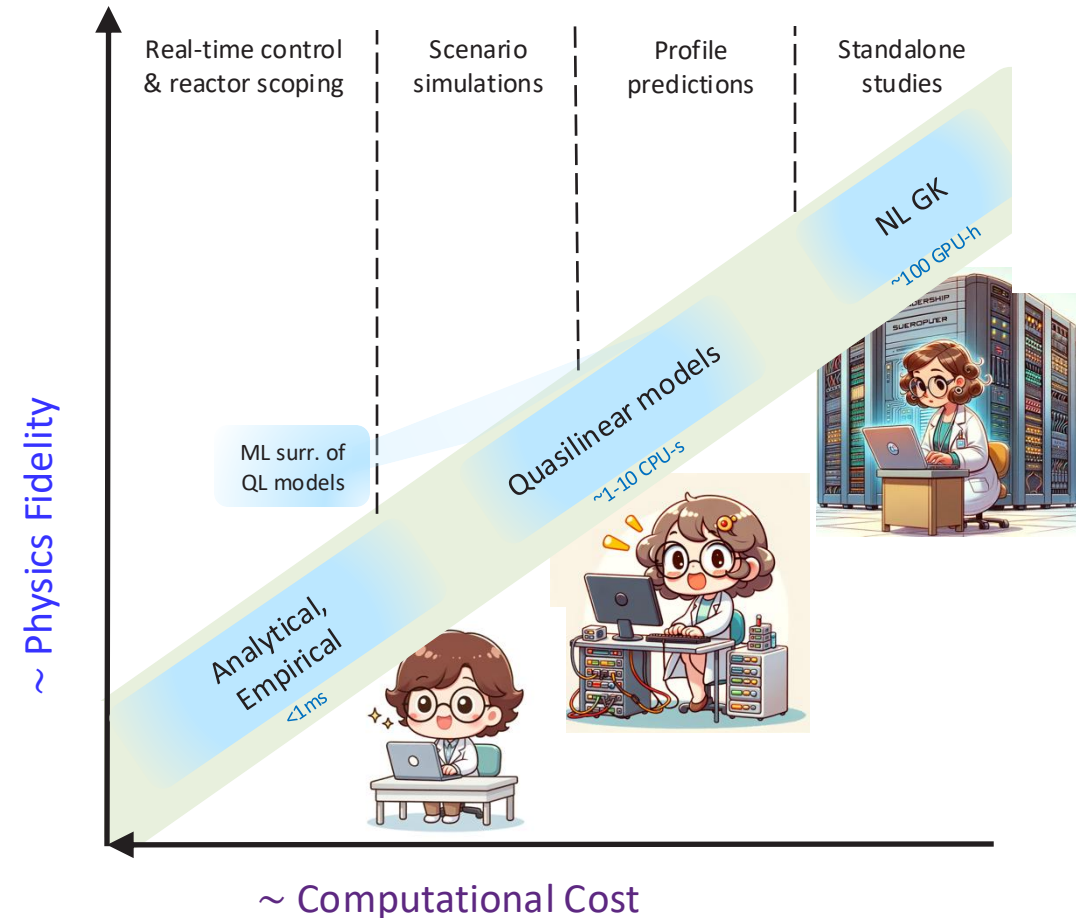
Predictive transport modeling is critical for effective FPP design

- Given a device design and operational parameters, fusion power production depends on transport processes.



- The characterization of the effect of transport phenomena is a clear trade-off between fidelity and cost:

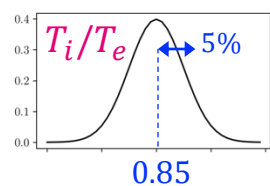
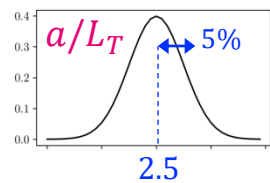
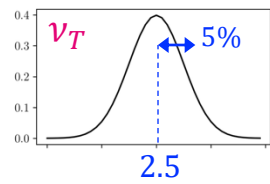
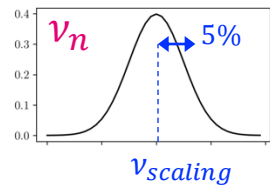
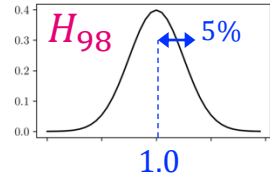
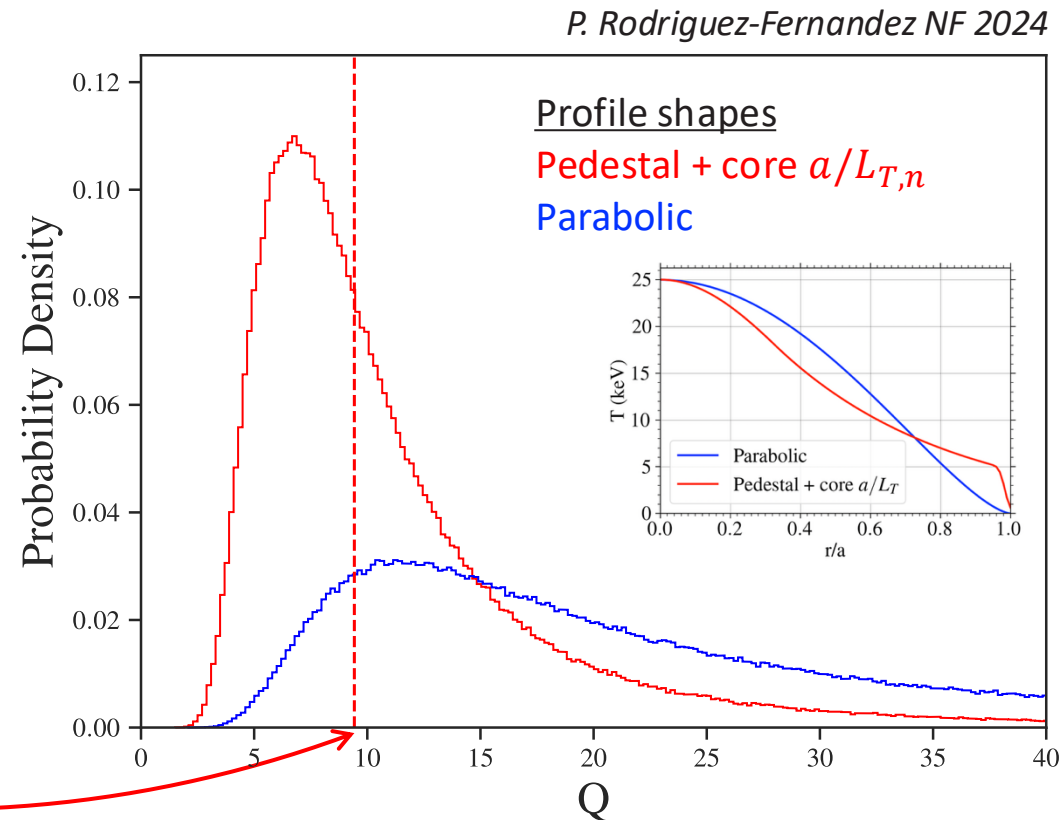
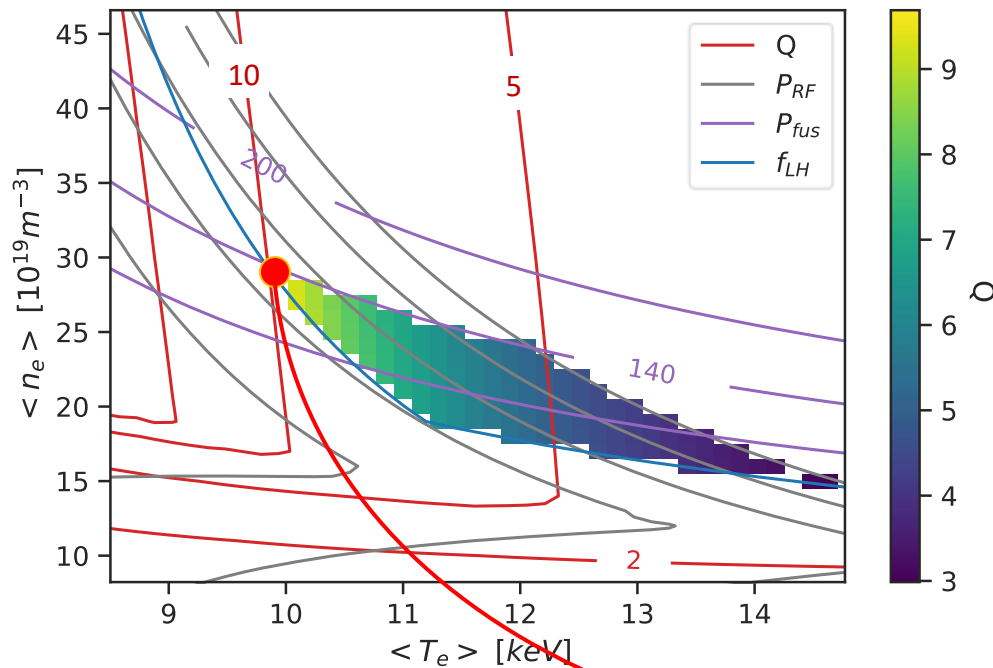
- Global energy confinement time (+ **H factor**) in **empirical workflows**.
- Critical gradient models (+ **parameters**) in **analytical workflows**.
- Quasilinear transport models (+ **saturation rule**) in **physics-based workflows**.
 - ML Surrogates (+ surrogate quality) in fast workflows.
- Gyrokinetic codes in **first-principles workflows**.



*Cartoon illustrations from chatGPT-4

0D power balance codes can arbitrarily choose performance

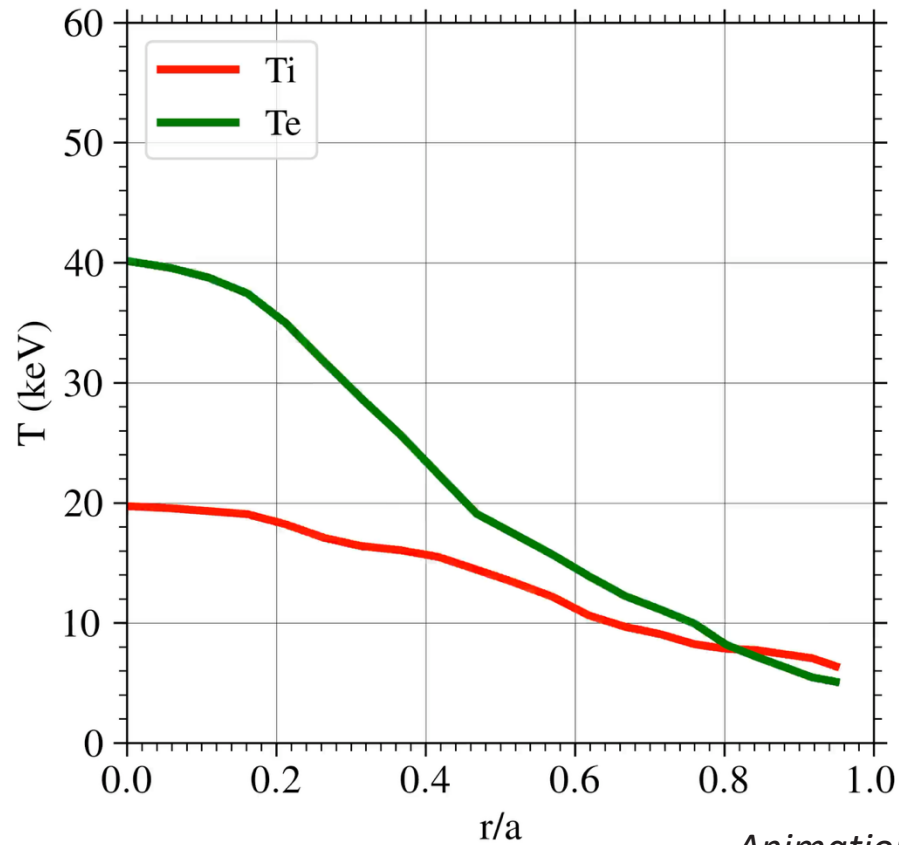
- Using energy confinement time from scaling laws is insufficient to predict tokamak performance.
- Uncertainties in transport-related input parameters to POPCONs or system codes result in **high variability** in predicted fusion power and fusion gain.



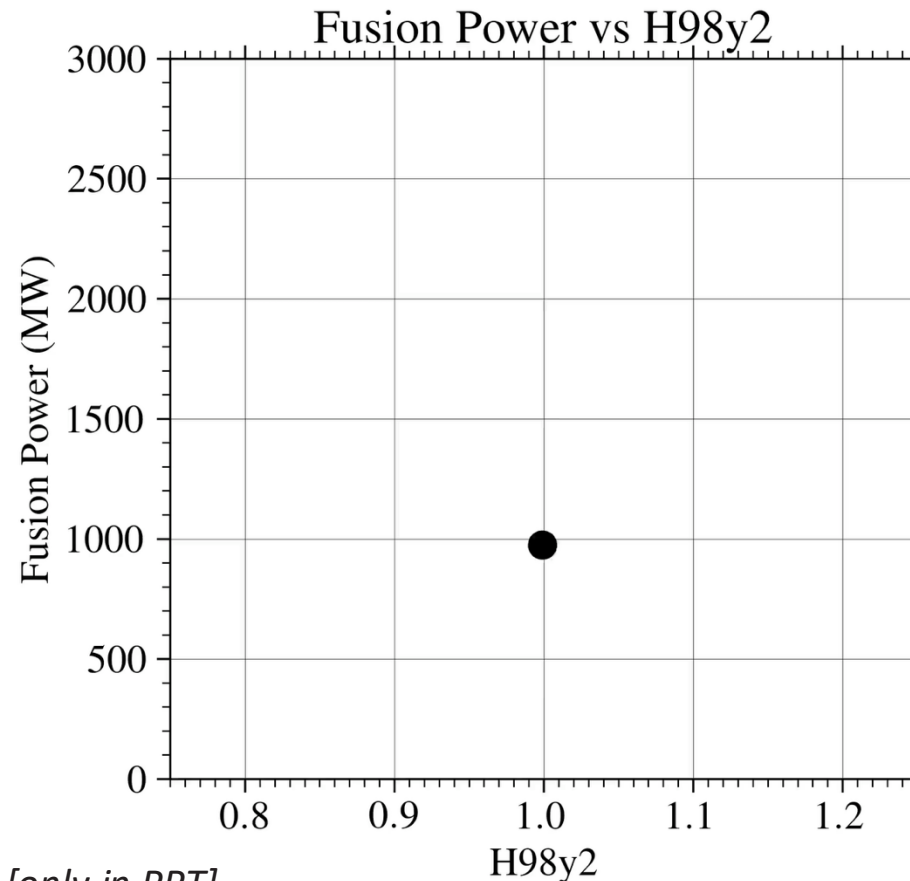
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ARC-class



Animation [only in PPT]



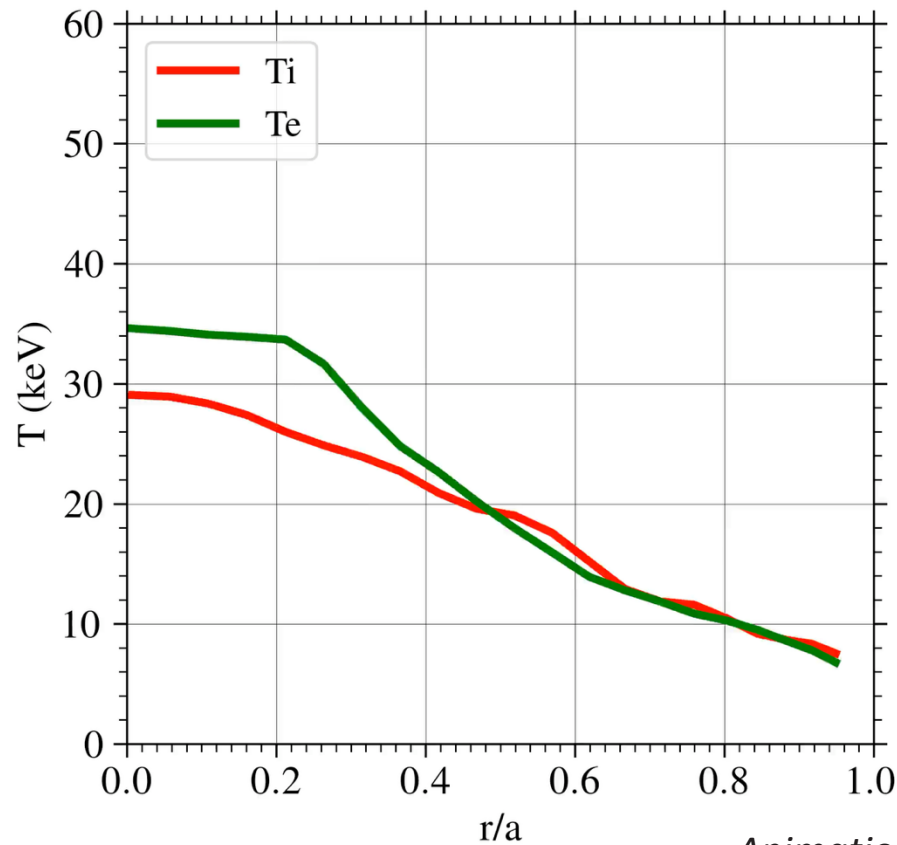
Exploratory study (random)

- $H_{98y2} \in [0.999, 1.001]$
- Fixed density

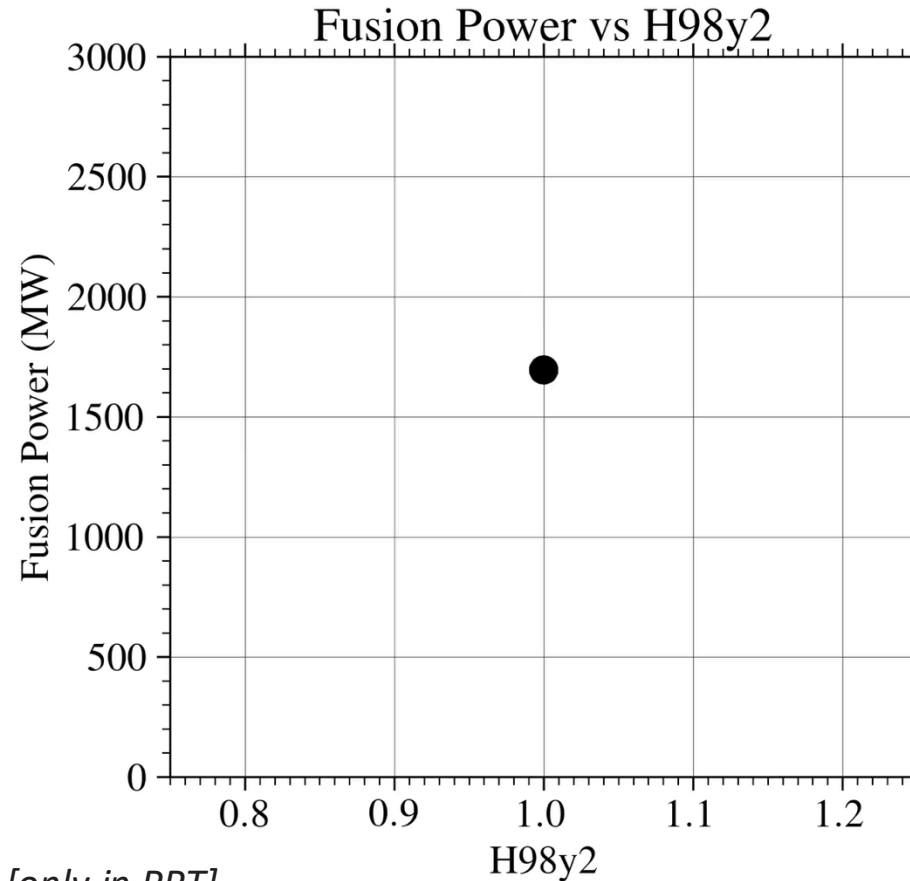
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Exploratory study (random)

- $H_{98y2} \in [0.999, 1.001]$
- Fixed density
- $\langle T_i \rangle / \langle T_e \rangle \in [0.8, 1.2]$
- $T_{i0} / \langle T_i \rangle \in [1.8, 2.5]$

Tokamak performance predictions are subject to numerous uncertainties

- In the scoping process of tokamak core performance, open questions still remain that add uncertainty in the modeling:
 - ❑ Impurity content
(sources, penetration, ash accumulation...)
 - ❑ Operational regime
(H-mode flavor, access, sustainment, ELMs...)
 - ❑ Boundary conditions
(edge pressure, temperature ratio, density gradients...)
 - ❑ Fast ion effects
(instabilities, interaction with turbulence...)
 - ❑ ...

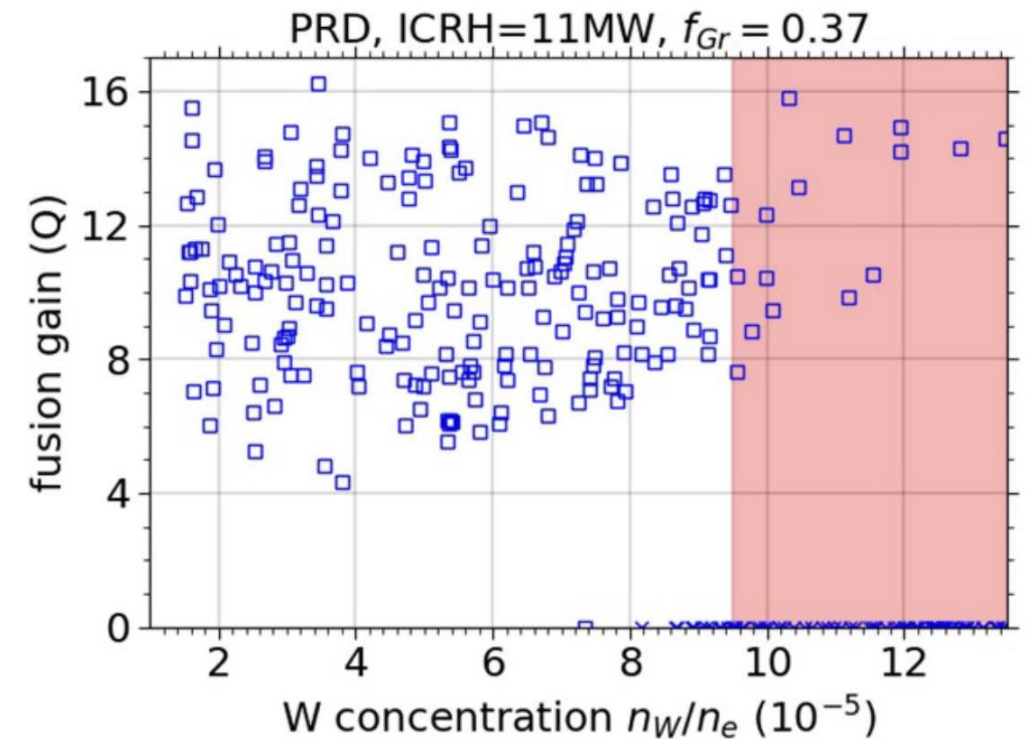
Assumption variations

$$f_W \in [1.5 - 13.5] \cdot 10^{-5}$$

$$f_{DT} \in [0.8 - 0.875]$$

$$T_i/T_e|_{ped} \in [0.8 - 1.2]$$

$$p_{top}/p_{EPED} \in [0.8 - 1.2]$$



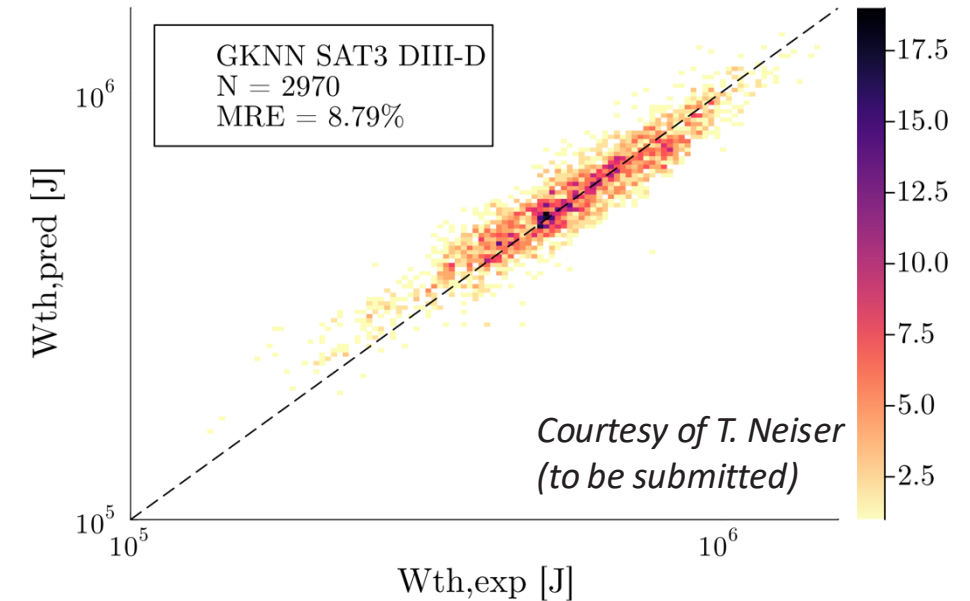
M. Muraca NF 2025

M. Muraca EU TTF 2025 [**Poster session 1**]

Transport model selection is a big lever for performance

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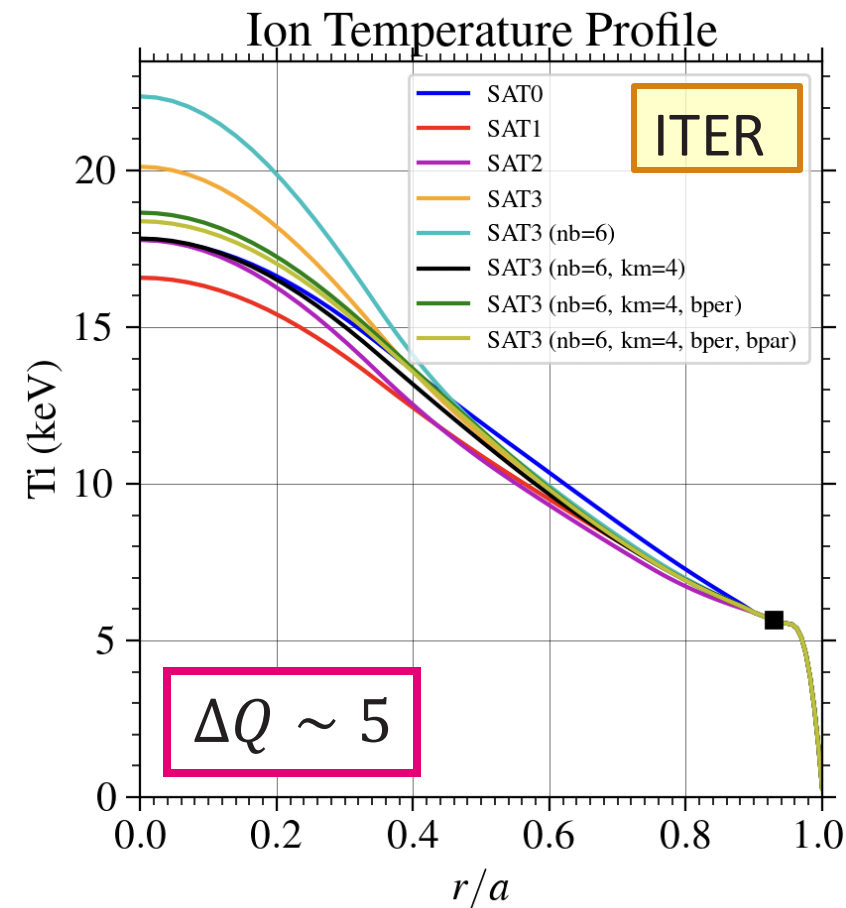
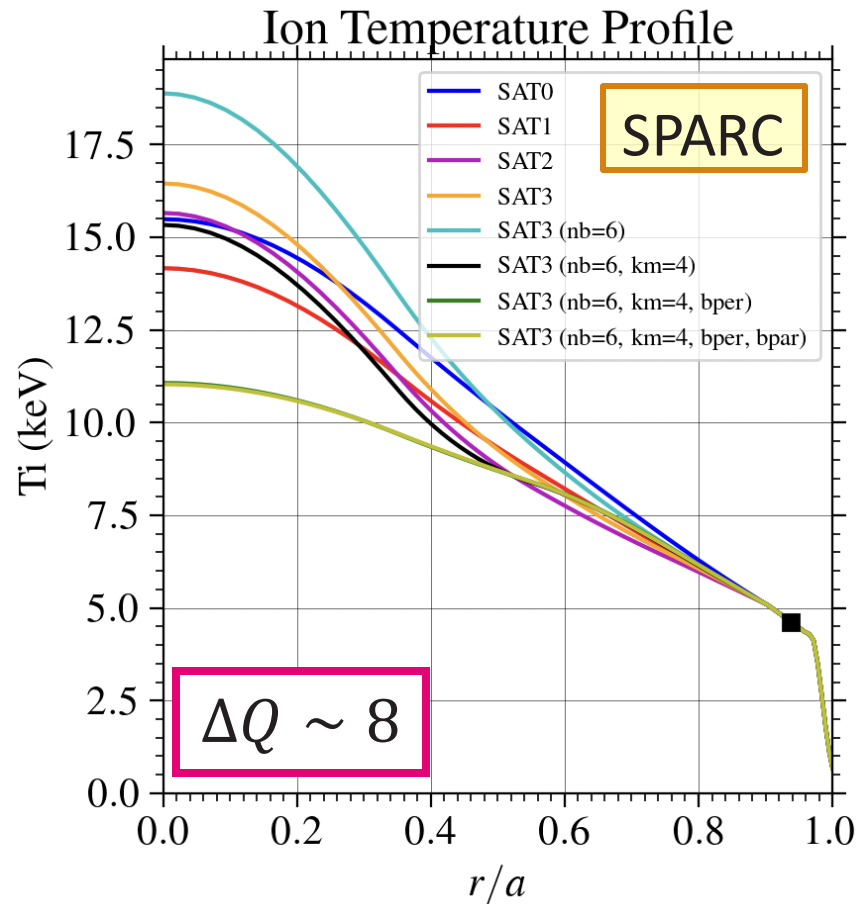


Device	H-mode	L-mode	negD
DIII-D	SAT0Q EM → GKNN SAT3 EM	SAT1 EM → GKNN SAT3 EM	SAT1 EM → GKNN SAT3 EM
MAST-U	SAT0Q EM → GKNN SAT3 EM	SAT3 EM → GKNN SAT3 EM	N/A
NSTX	SAT3 EM → GKNN SAT3 EM	SAT3 EM → GKNN SAT3 EM	N/A

- While it is widely assumed that the nonlinear gyrokinetic model captures core transport with enough fidelity, the assumptions in integrated modeling with **quasilinear models** introduce a large **additional** uncertainty.

Burning plasma & power plant projections sensitive to turbulence saturation

- Predictions of SPARC and ITER, even at fixed BC, can differ substantially depending on what model to use.



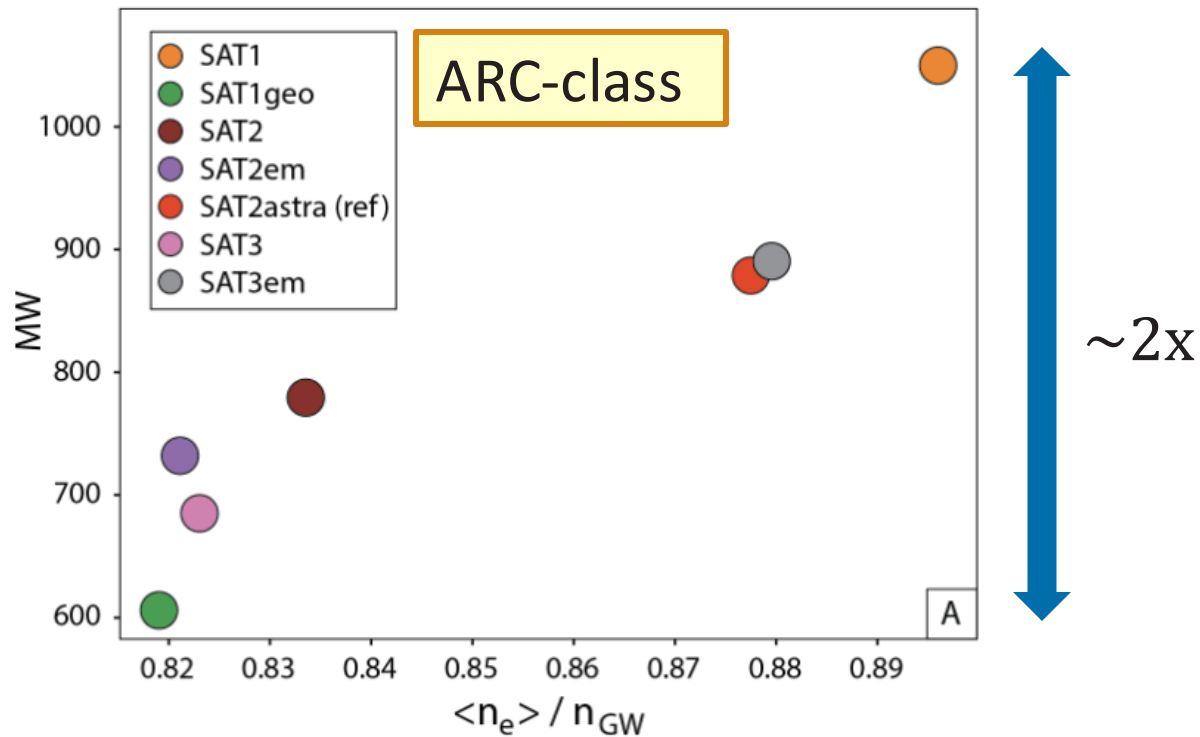
Parameters and assumptions for SPARC PRD plasma as in *P. Rodriguez-Fernandez NF 2024*

ITER Baseline plasma (Be) as in *N. Howard NF 2025*

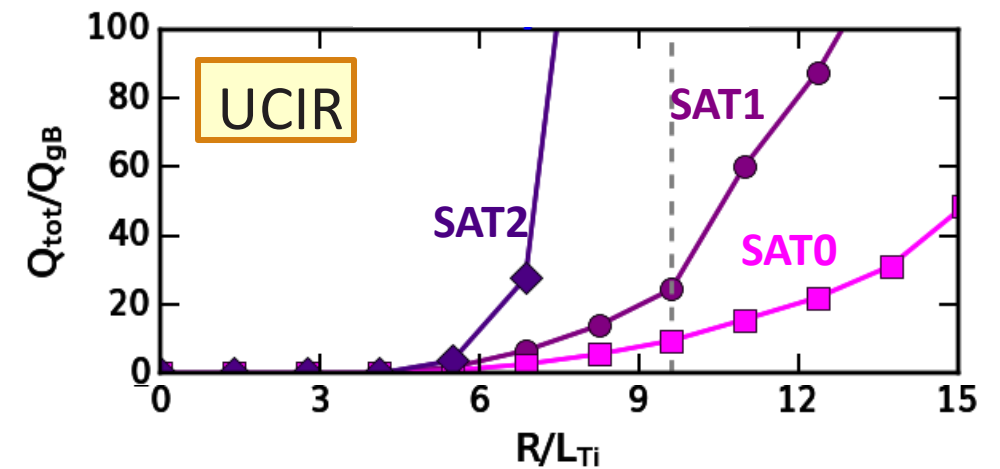
Burning plasma & power plant projections sensitive to turbulence saturation

- Predictions of SPARC and ITER, even at fixed BC, can differ substantially depending on what model to use.
- FPP predictions (plasmas strongly on burning regime) are particularly affected by model selection.

N. Howard (to be submitted)



C. Holland APS-DPP 2021

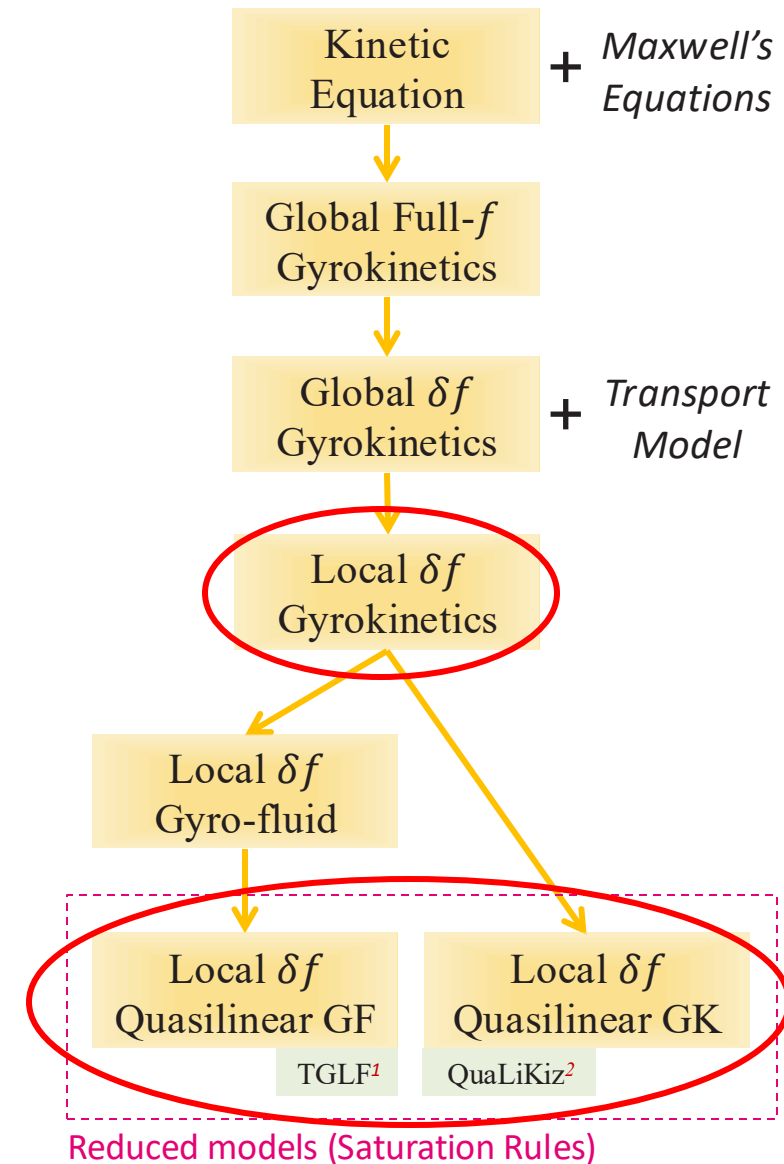


Core model selection hierarchy represents a cost vs. fidelity trade-off

- A **hierarchy of assumptions** has been developed to reduce computational cost from the full- f , 6D + time, kinetic description.
- The jump from nonlinear to reliable **quasilinear models** has made integrated modeling possible ($\sim 10^6$ cost savings with reasonable results).
- In predicting burning plasmas and selecting robust FPP designs, we require **validation** and spot checks with higher fidelity turbulence simulations.
- **New era in core transport research**: the direct use of NL GK to predict kinetic profiles and performance and aid in the design of fusion devices.

Demonstration of high-fidelity solvers in 2022:

- ❑ **PORTALS-CGYRO (MIT)** – Rodriguez-Fernandez, Howard & Candy
- ❑ **TANGO-GENE (IPP)** – Di Siena, Jenko, et al.
- ❑ **TRINITY-GX (PPPL)** – Dorland, Mandell, et al.



¹G.M. Staebler PoP 2007

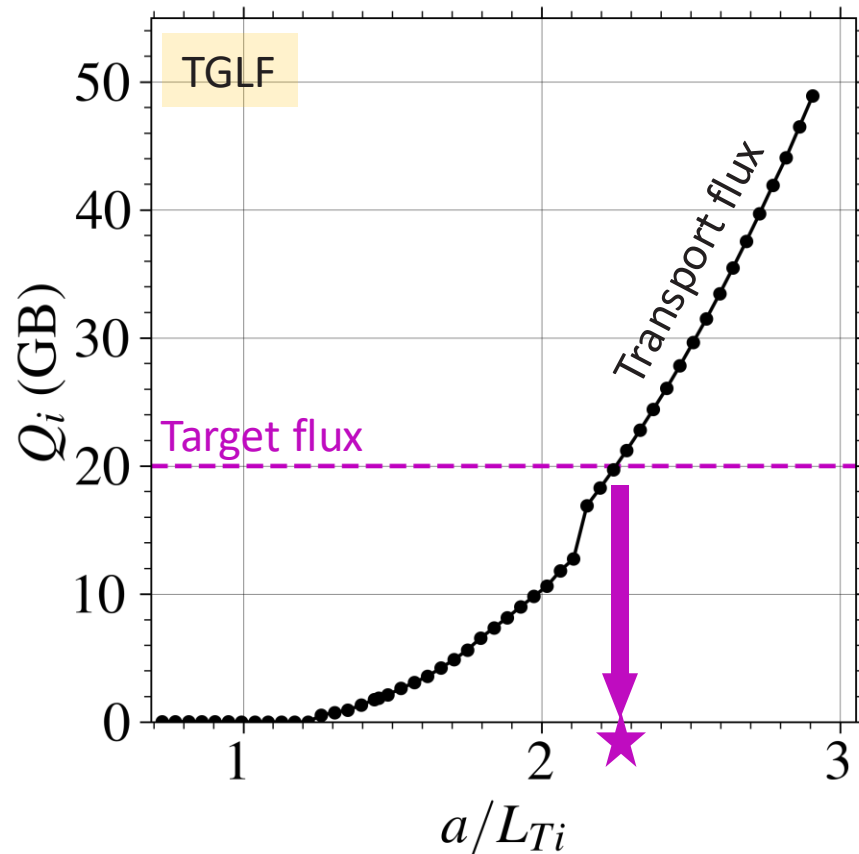
²C. Bourdelle PPCF 2015

Practical predictions require an inverse solver for δf turbulence codes

- Solving for the steady-state plasma using local, δf transport models requires solving an inverse problem.

$$\frac{1}{V'} \left[\frac{\partial}{\partial t} \left(\frac{3}{2} n_i T_i V' \right) + n_i T_i \frac{\partial V'}{\partial t} \right] = - \frac{1}{V'} \frac{\partial}{\partial r} (\langle q_i \cdot \nabla r \rangle V') + \langle S_i \rangle \quad \longrightarrow \quad \langle q_i \cdot \nabla r \rangle = \frac{1}{V'} \int_0^r \langle S_i \rangle V' dr$$

$$Q_i^{TRANSPORT} = Q_i^{TARGET}$$

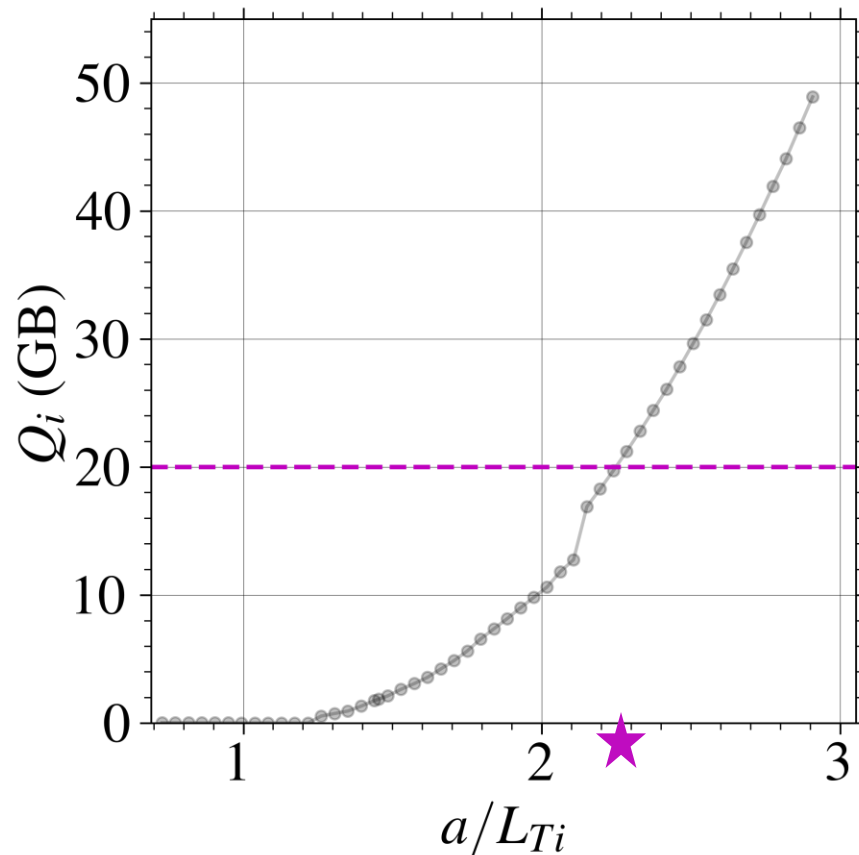


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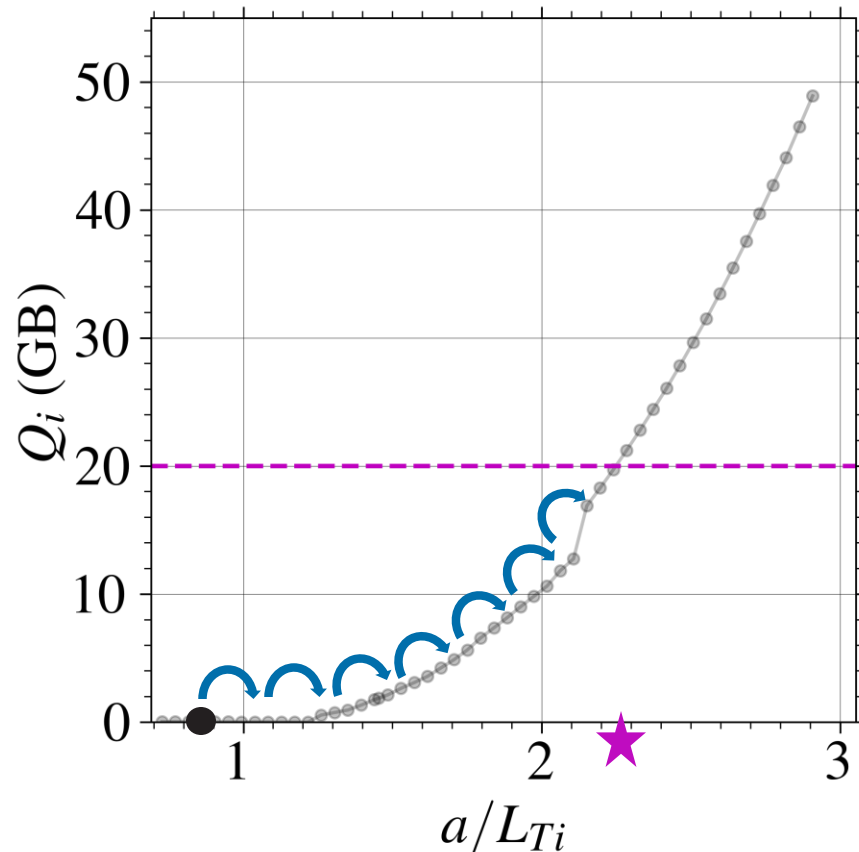


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- Standard transport solvers find the steady-state solution via small, stable “steps” towards reducing a residual (time-indep.) or dW/dt (time-dep.).
- Jacobian calculation, use of small steps or ad-hoc modifications of flux response (numerical diffusivity) to achieve convergence is often too costly* to use with **nonlinear gyrokinetics**.
- This work was pioneered by:
 - J. Candy et al., Phys. Plasmas (2009) [TGYRO + GYRO]
 - M. Barnes et al., Phys. Plasmas (2010) [TRINITY + GENE/GS2]

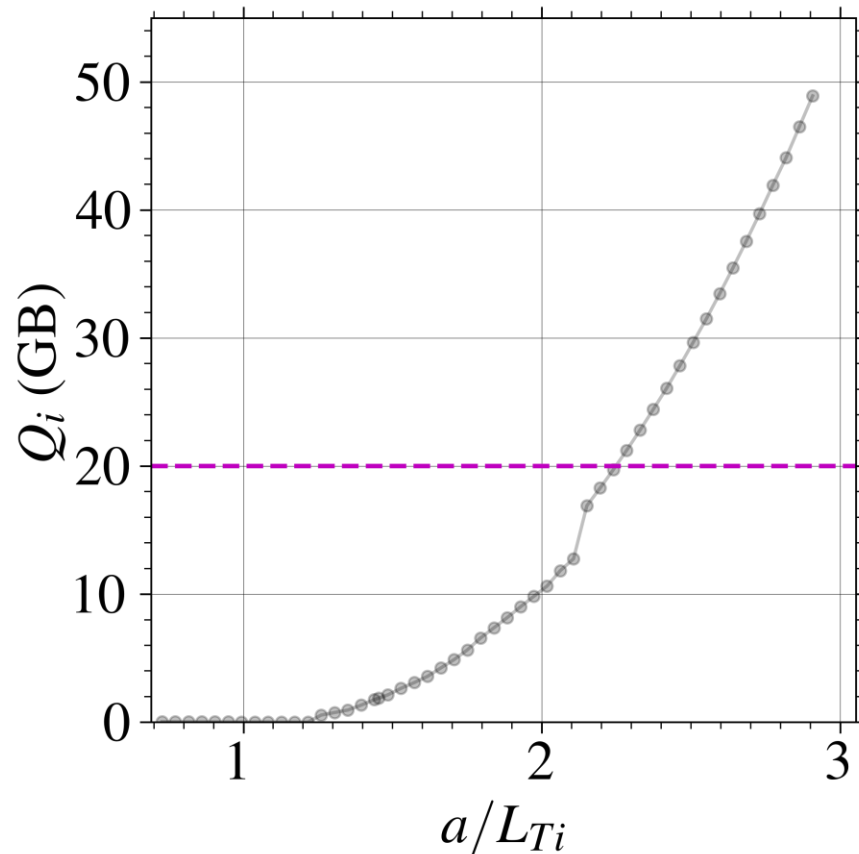
*Usually $10^2 - 10^3$ evaluations required in standard transport solvers

PORTALS: using surrogates for smarter sampling of the parameter space

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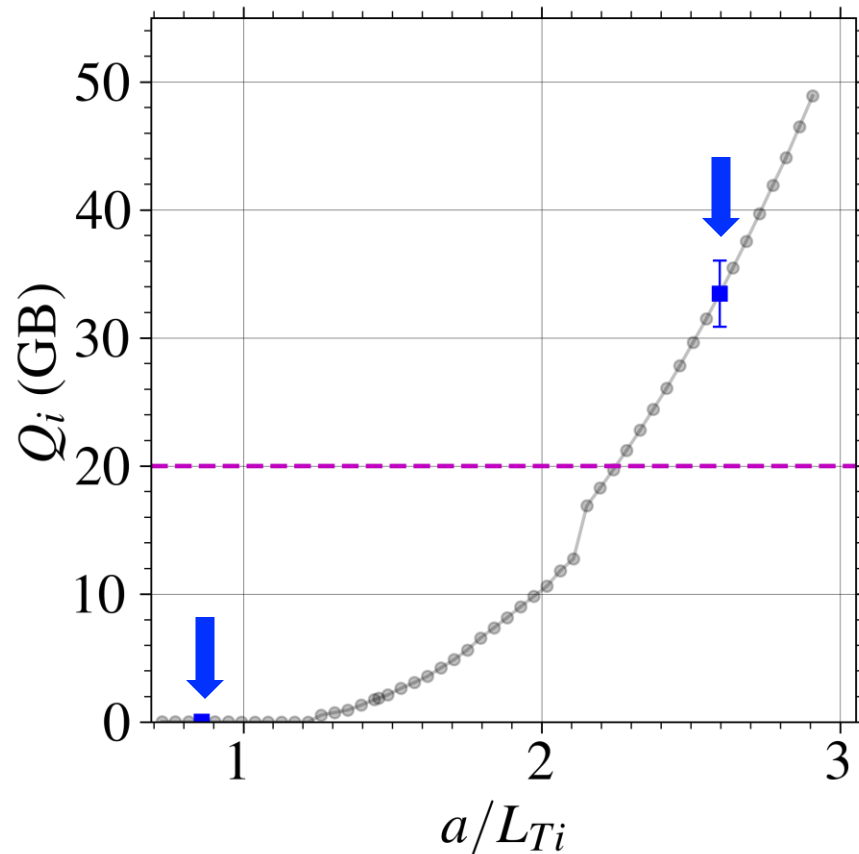
P. Rodriguez-Fernandez et al 2022 Nucl. Fusion 62 076036
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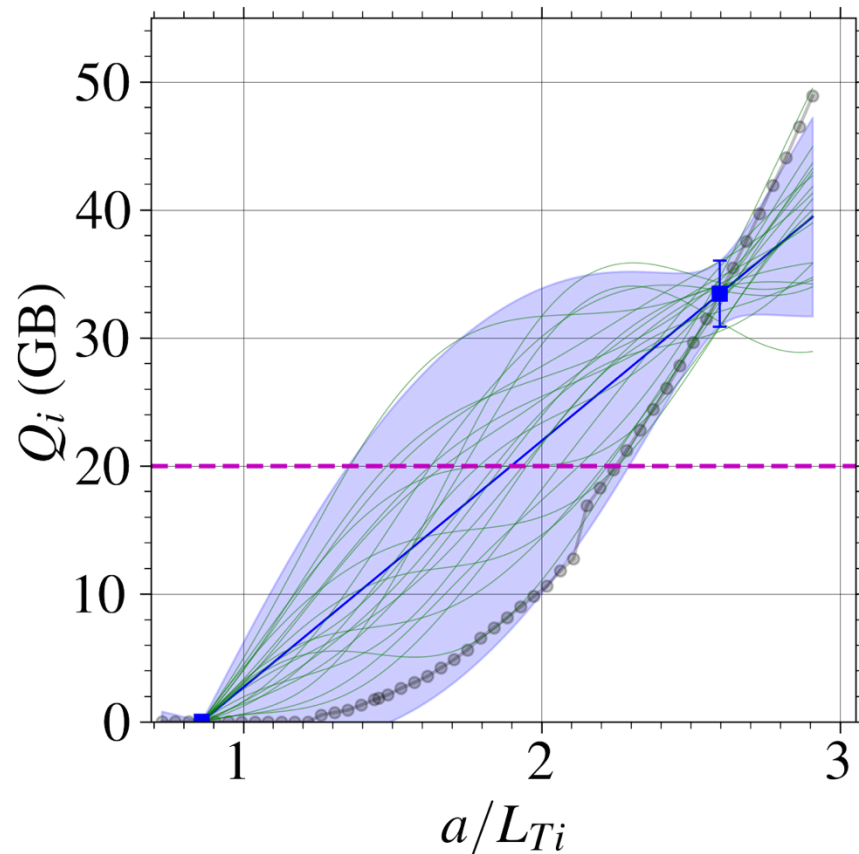
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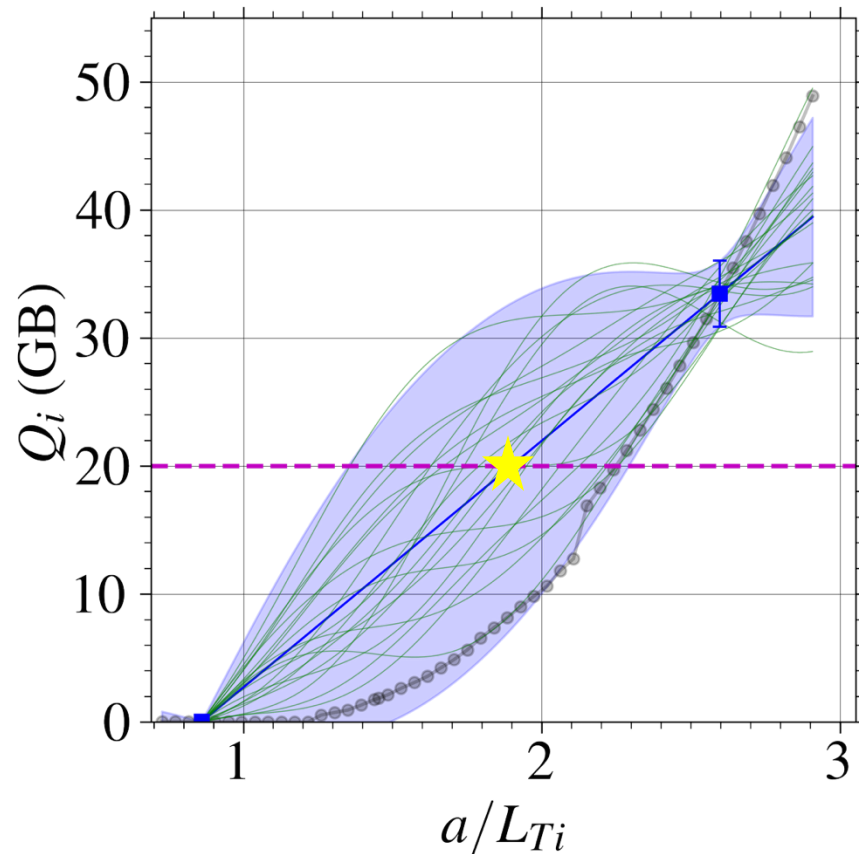
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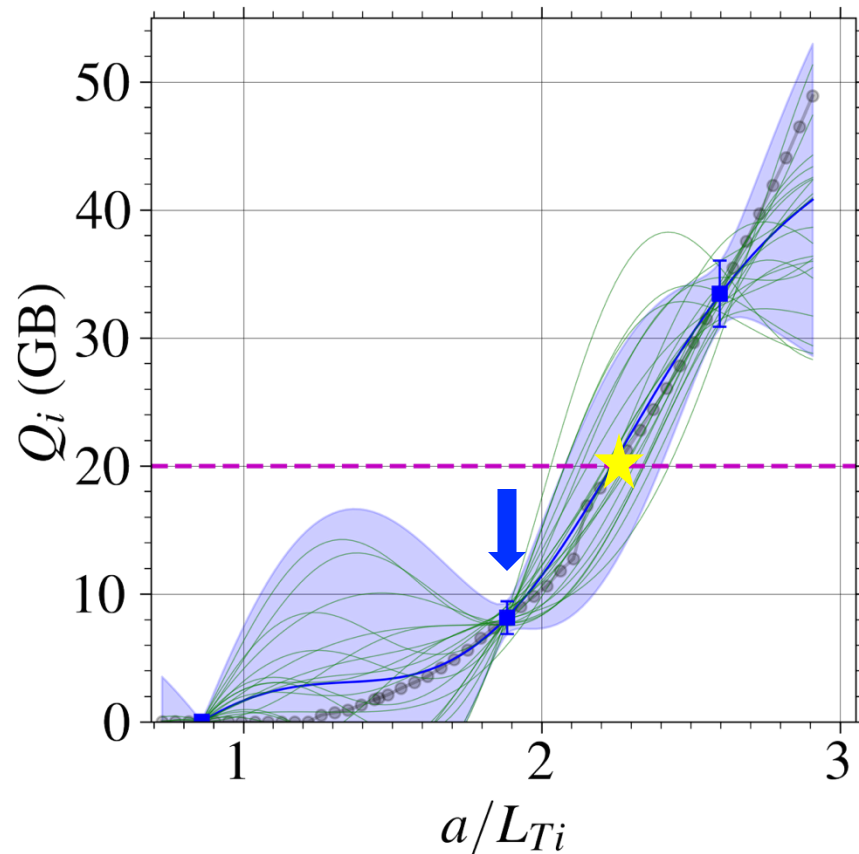
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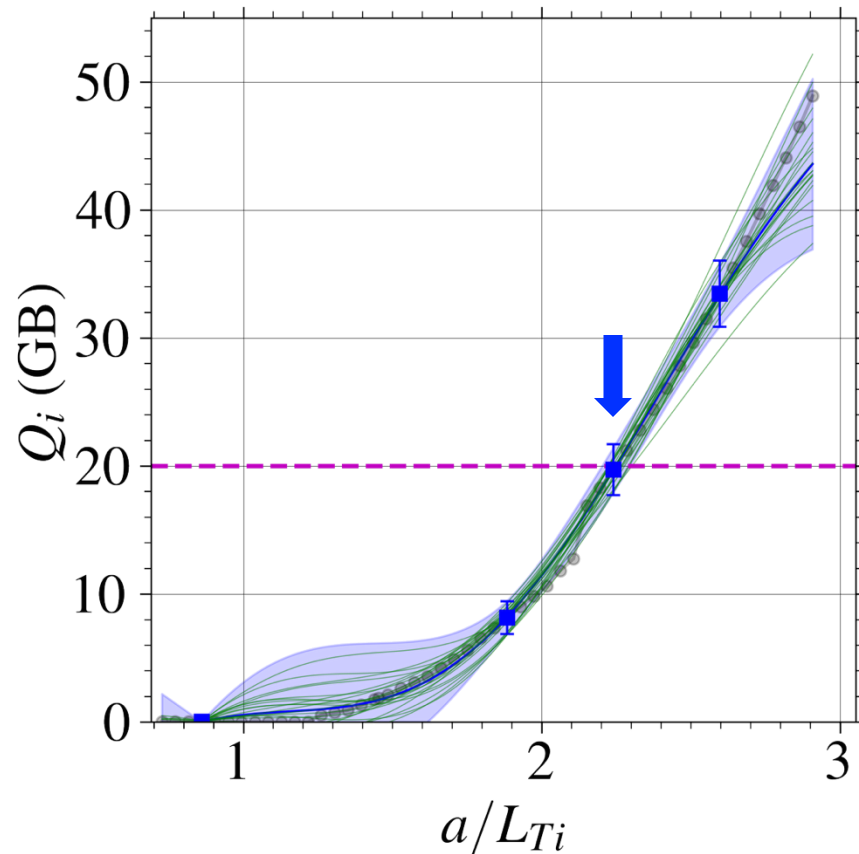
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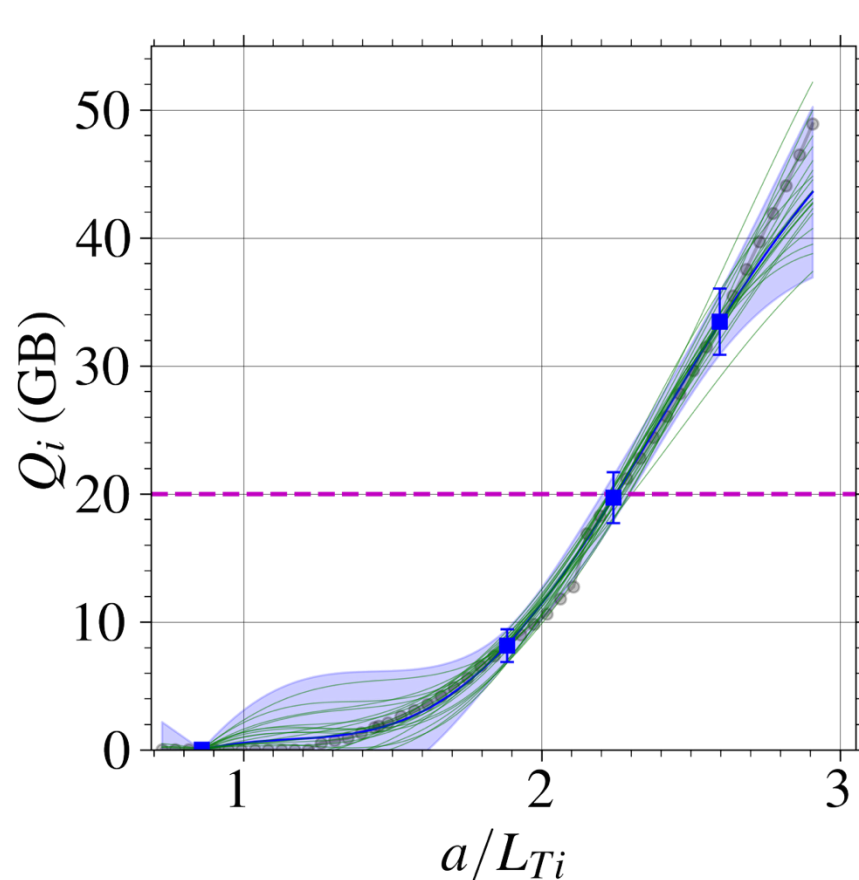
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This is the basis of what PORTALS does but... *a bit more complex...*

- + Multi-radius (radial coupling)
 - + Multi-channel (channel coupling)
 - + Multi-model (neoclassical + turbulence) → surrogate separation
 - + Moving-targets (volumetric flows) → targets as surrogates too
 - + GB-normalized transport → nonlinear transformations, MC surrogate
 - + Discontinuous, critical gradient or turbulence saturation → UQ
- } multi-objective, multi-variable

Because we evaluate the flux with the actual transport model (surrogates are just used to inform where to evaluate), PORTALS predictions are **NOT surrogate predictions** but actual transport model predictions.

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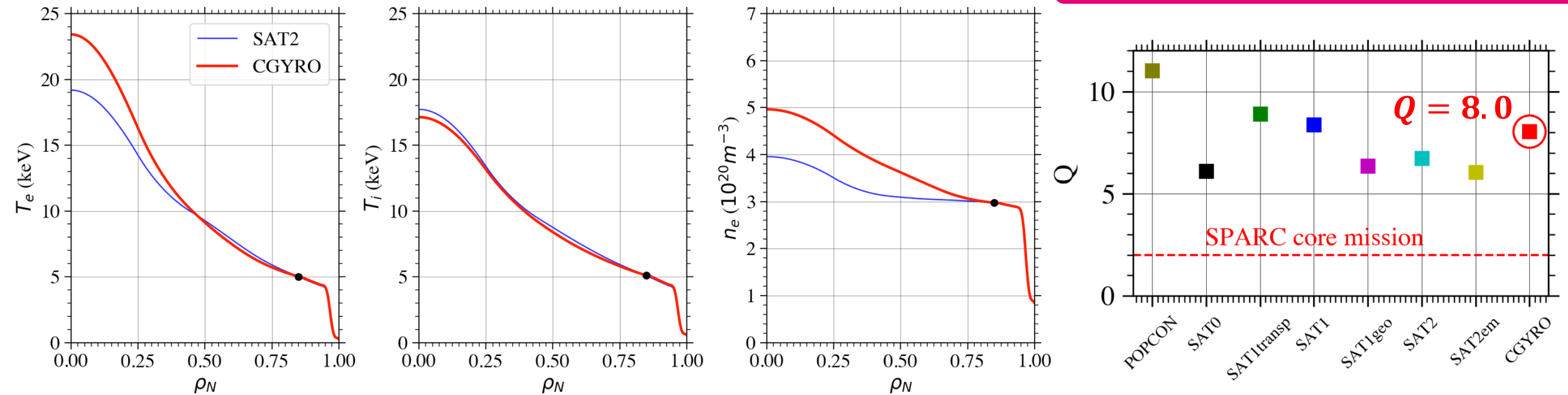
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SPARC PRD scenario was the first one to be simulated with PORTALS

- SPARC's PRD core simulations with PORTALS-CGYRO made SPARC the **first burning plasma predicted with core nonlinear gyrokinetics**.
- Only 16 profile evaluations $\rightarrow Q \approx 8.0$ prediction at ELMy H-mode pedestal levels.

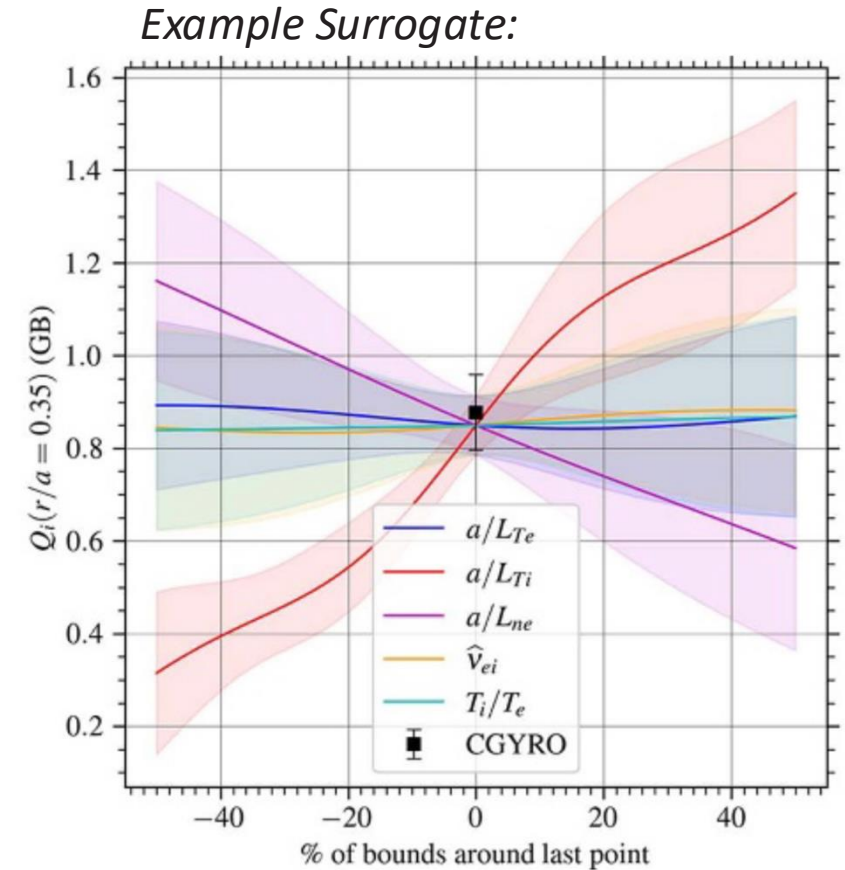
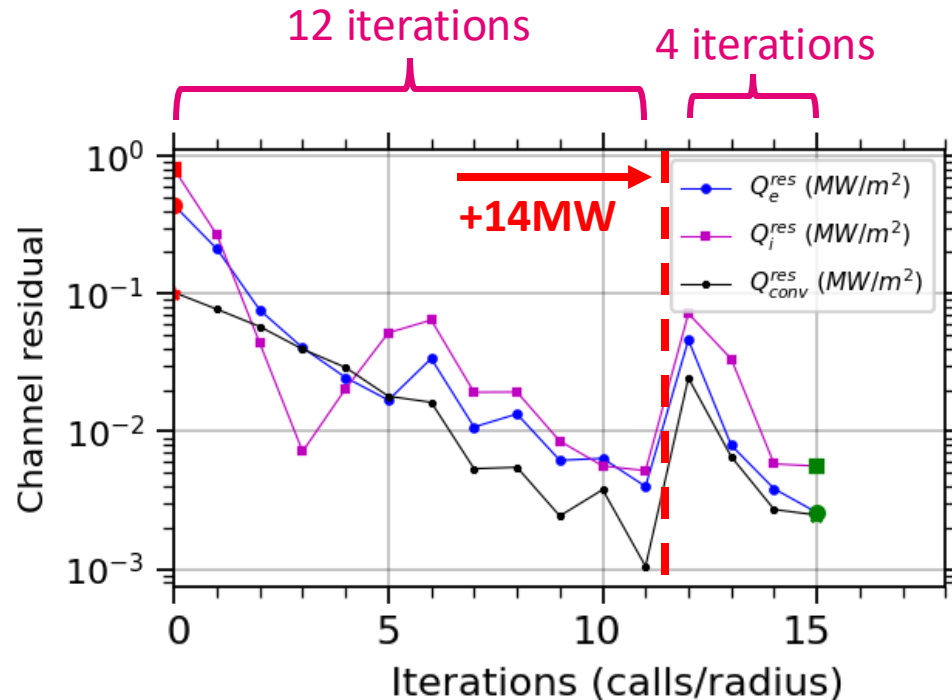
Physics included

- Multi-channel (T_e, T_i, n_e).
- Evolving alpha heating, energy exchange, radiation (Bremss, line, sync).
- NL CGYRO¹: EM, 6 GK species, Miller geometry, Sugama collisions, $k_\theta \rho_s \leq 1.2$.



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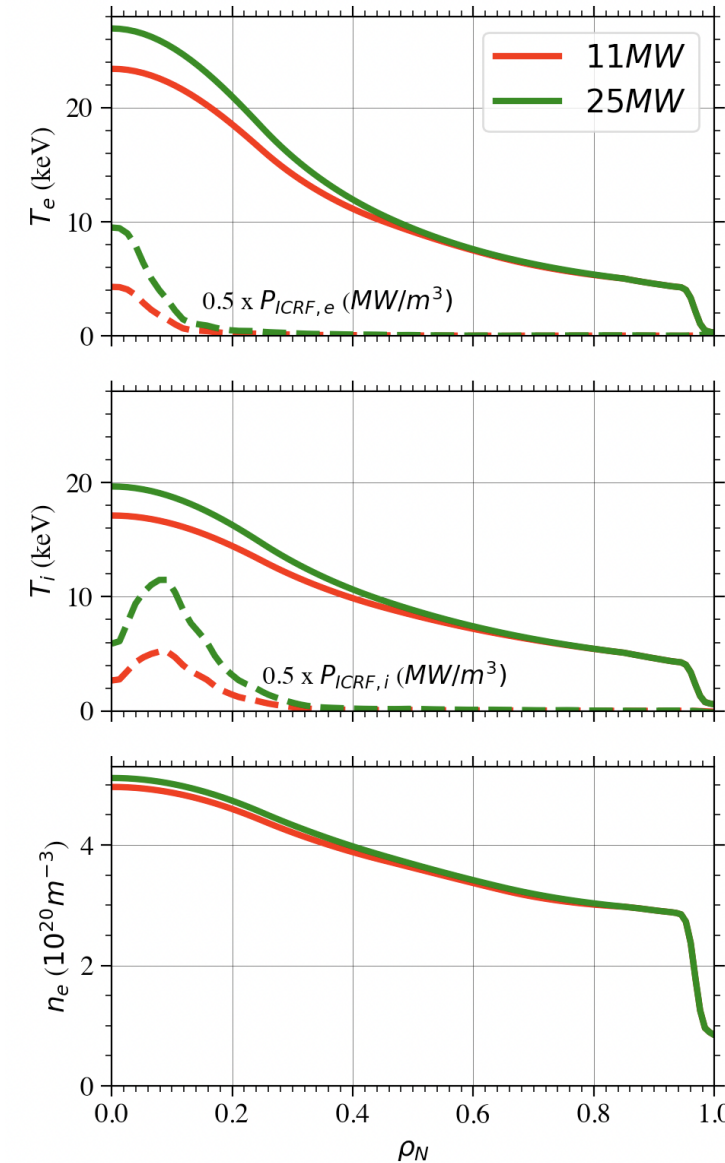
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Since surrogates are fitted to local parameters, targets (e.g. P_{ICH}) can be varied to obtain new flux-matched solution at reduced cost.

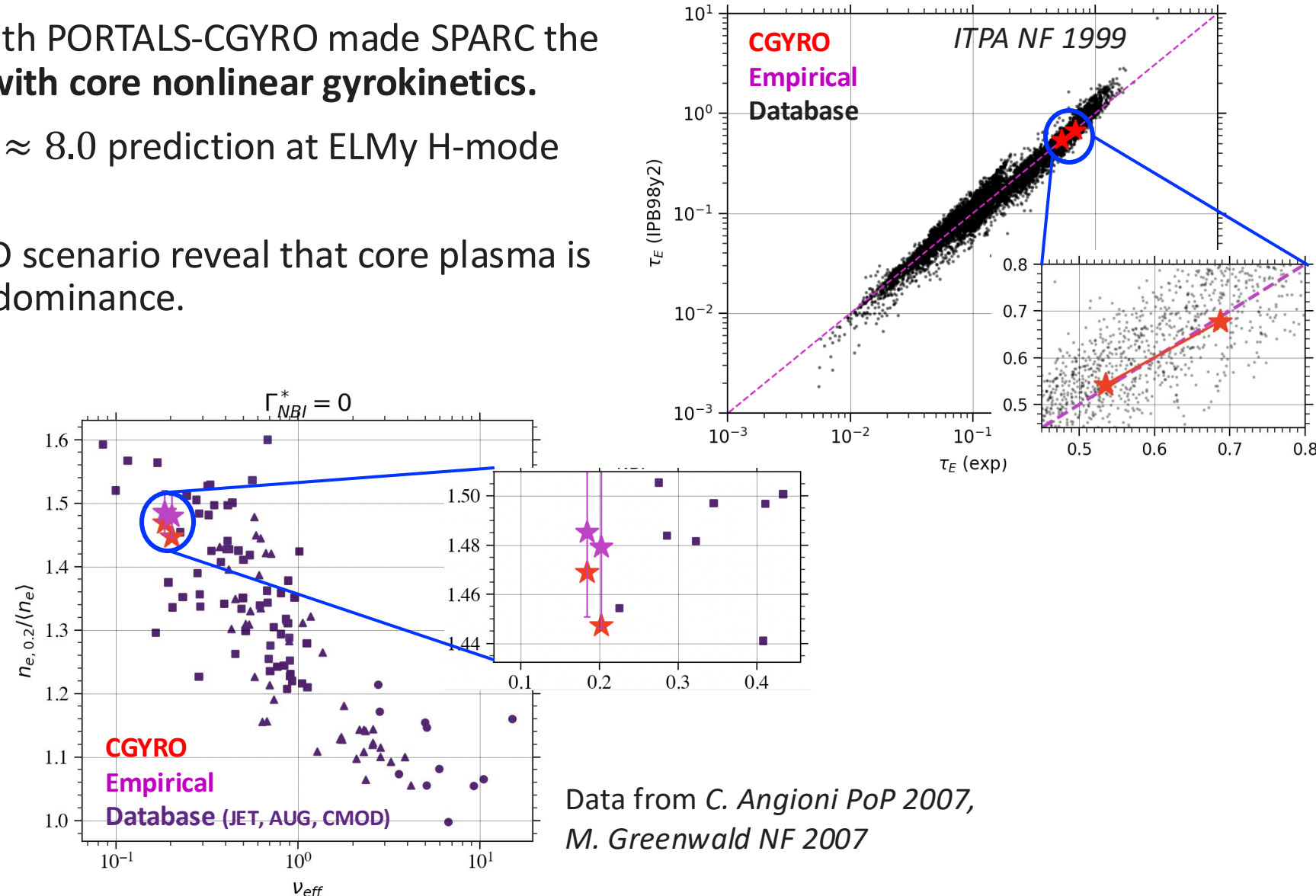
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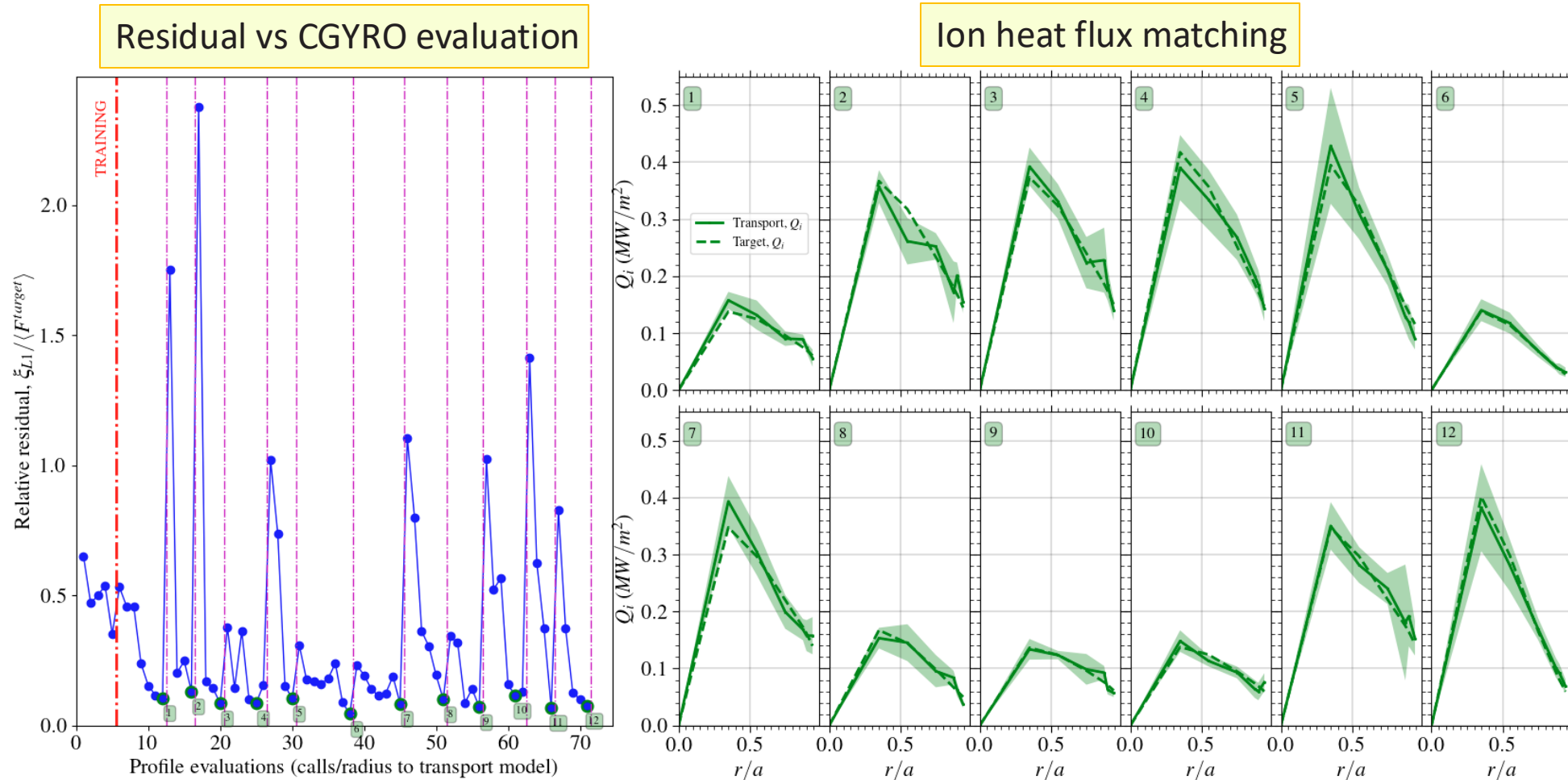
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- Predictions of SPARC 25MW-PRD scenario reveal that core plasma is **very stiff**, as expected from ITG dominance.
- In agreement with empirical scaling laws of global quantities.



Re-utilization of surrogates very advantageous for space exploration

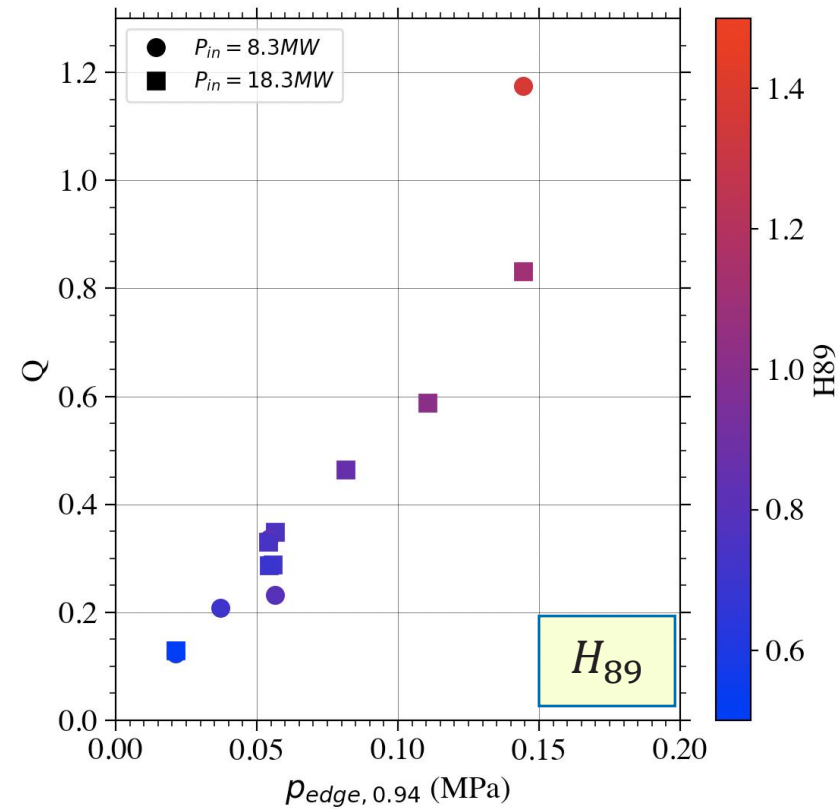
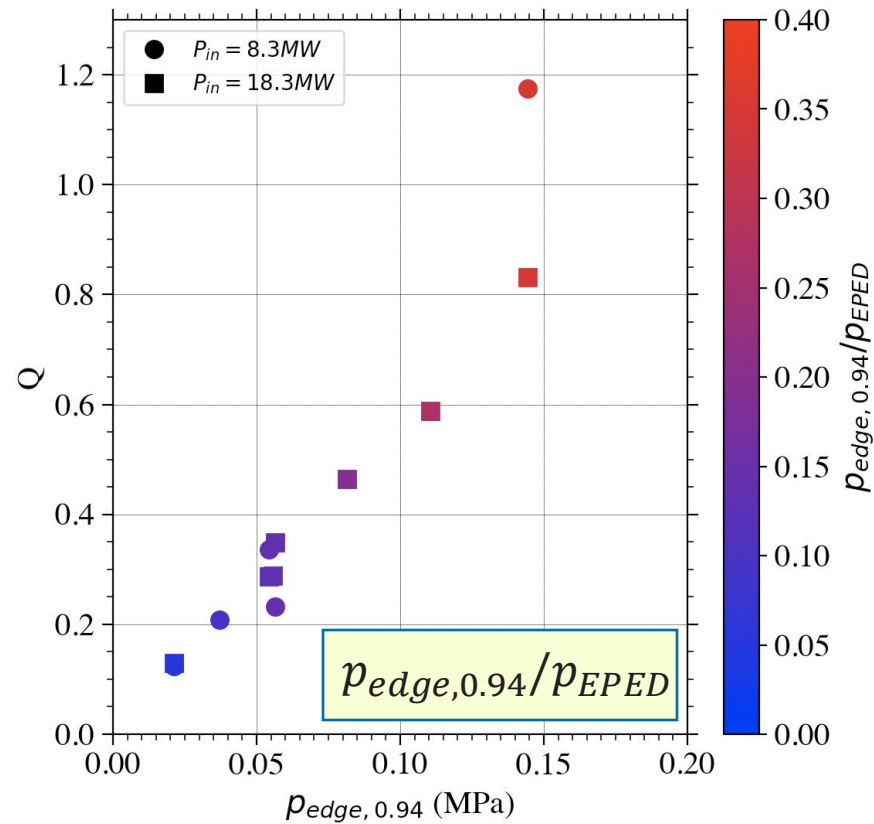
- Increased interest in $Q > 1$ in early campaigns required scoping of lower edge pressure and heating scenarios.
- 12 scenarios** (varying $T_{0.94}$, $n_{0.94}$, P_{ICH}) were predicted with 71 profile evaluations*.



*426 local CGYRO
80k GPU hours
Perlmutter (NERSC)

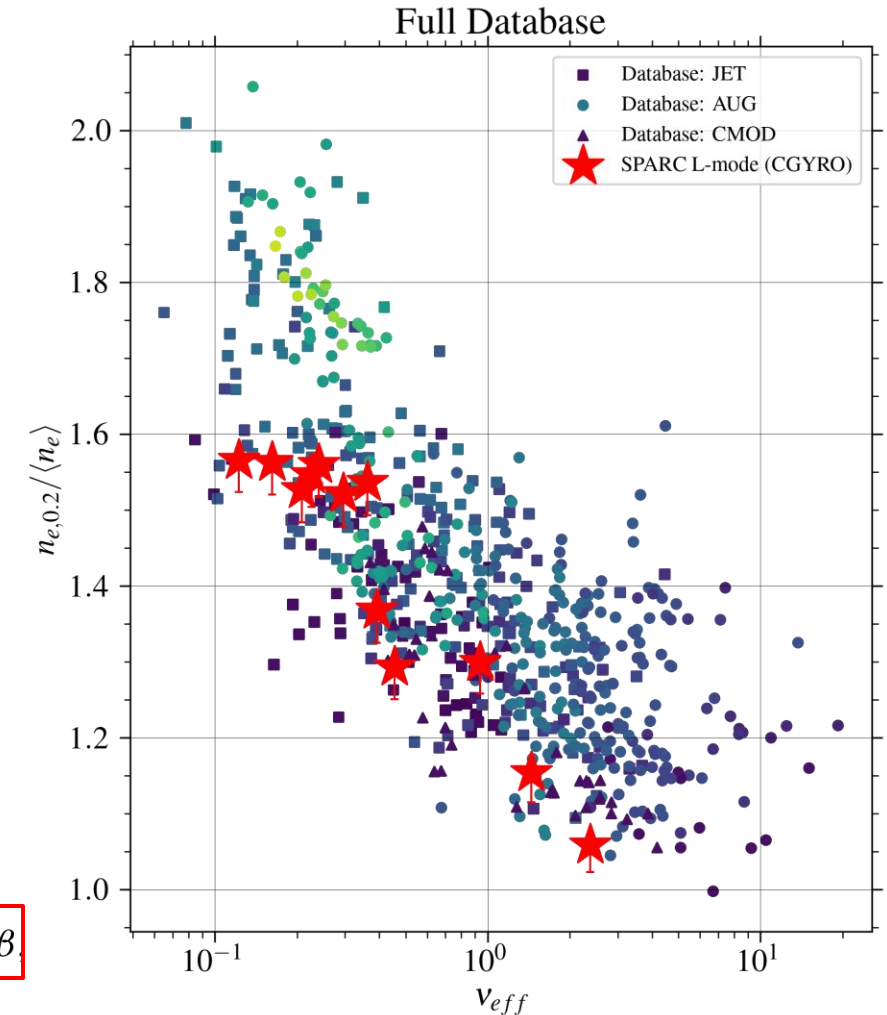
Pressure pedestal identified as key for breakeven

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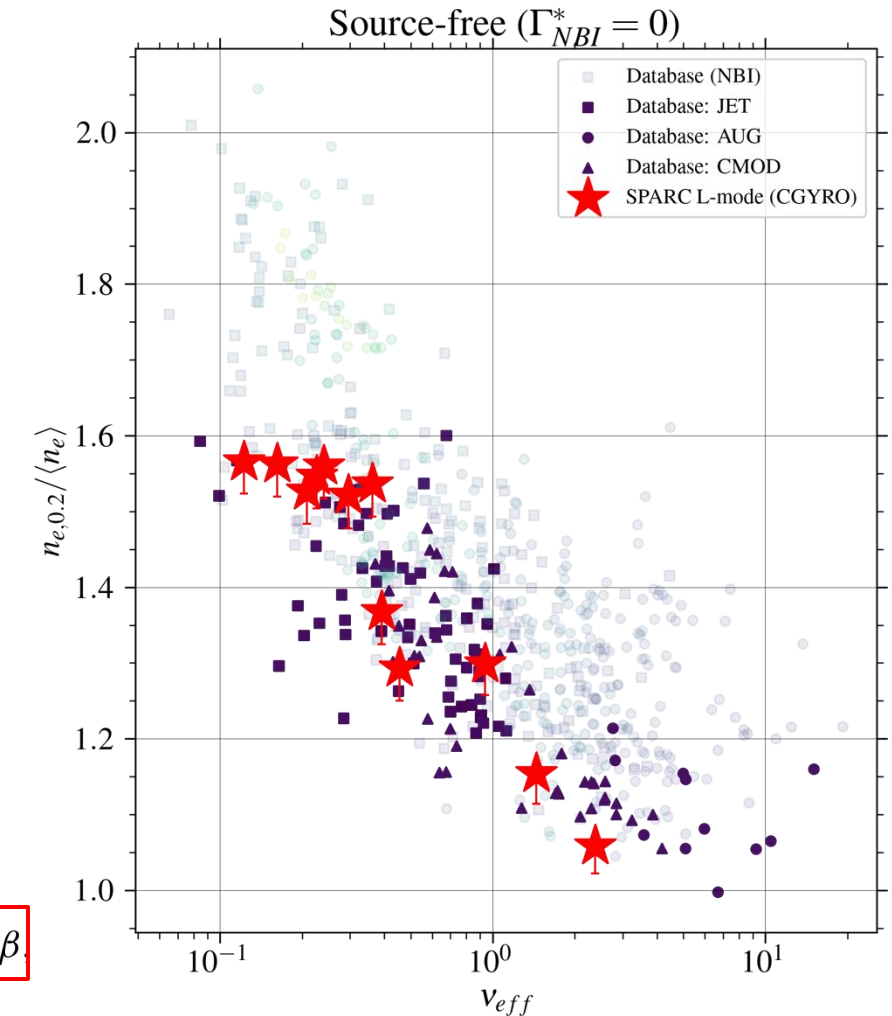


C. Angioni NF 2007, M. Greenwald NF 2007

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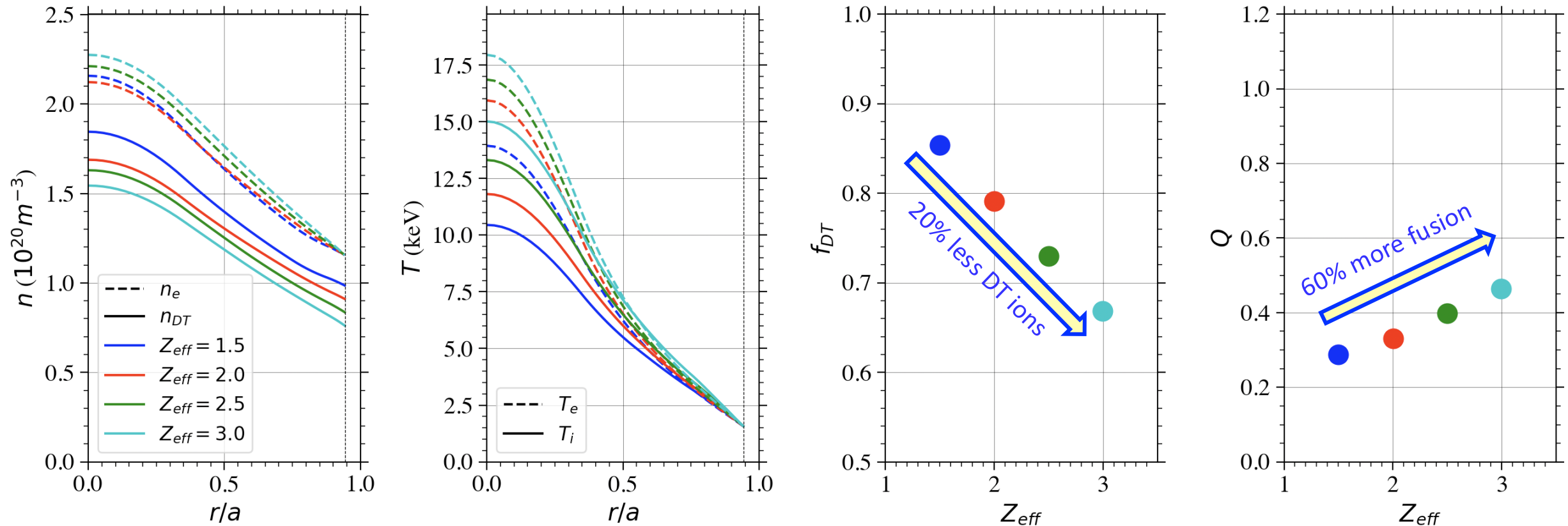


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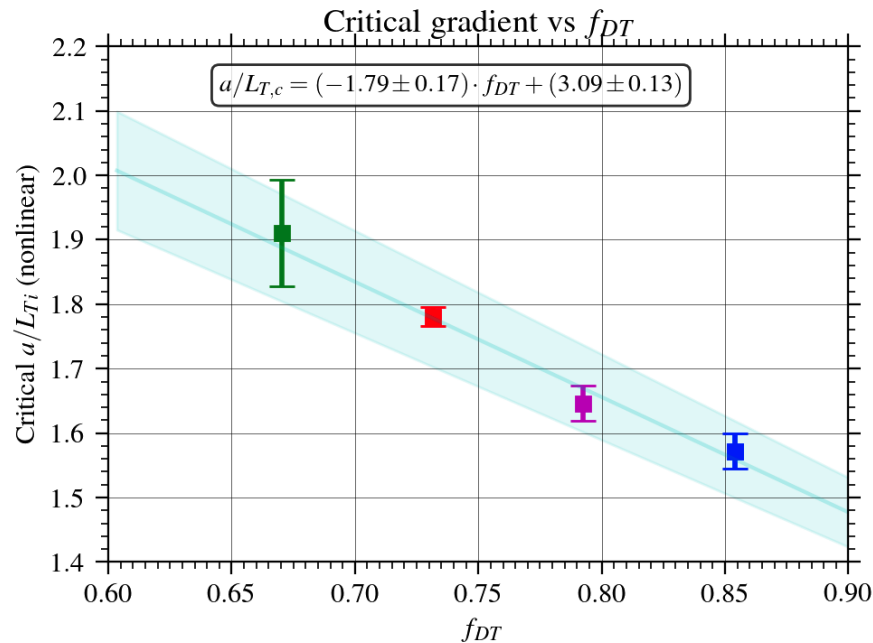
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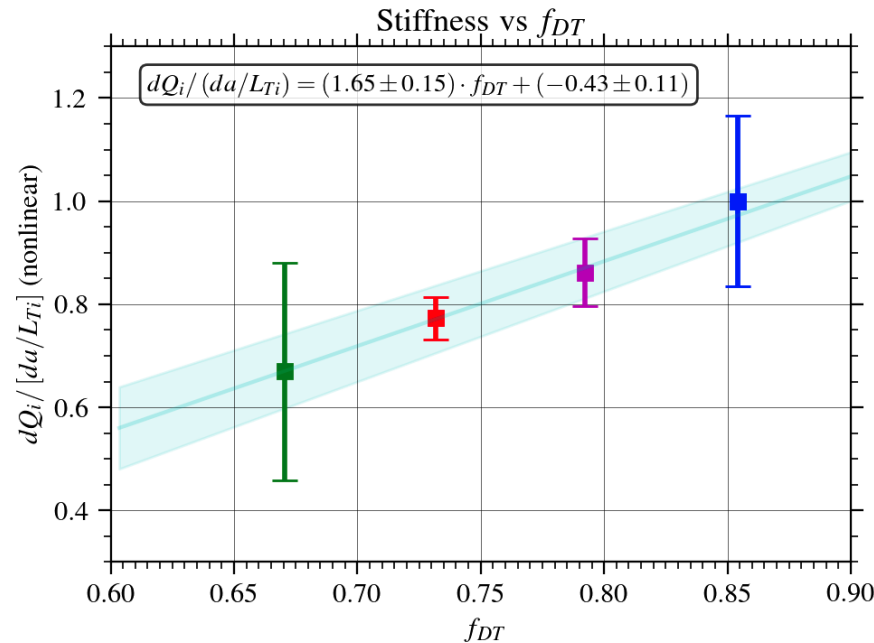


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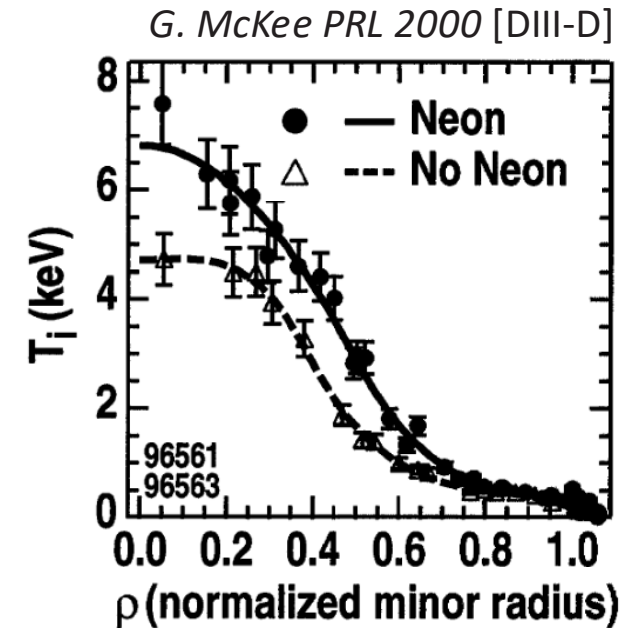
ITG critical gradient **increases**
with more diluted DT



Transport stiffness **decreases**
with more diluted DT

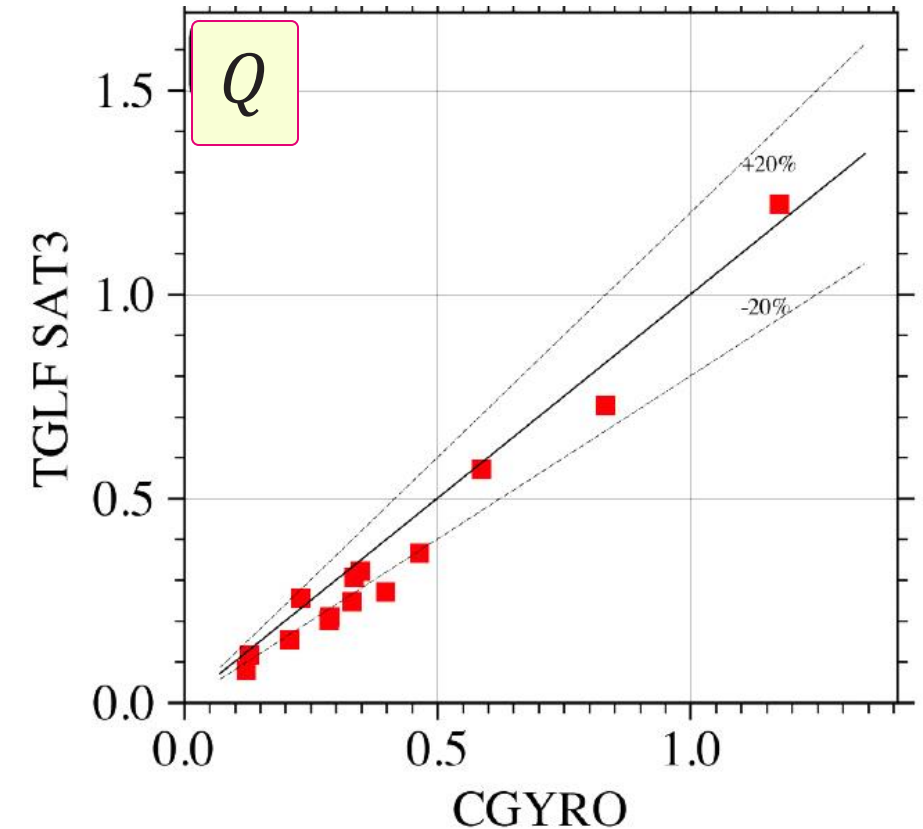
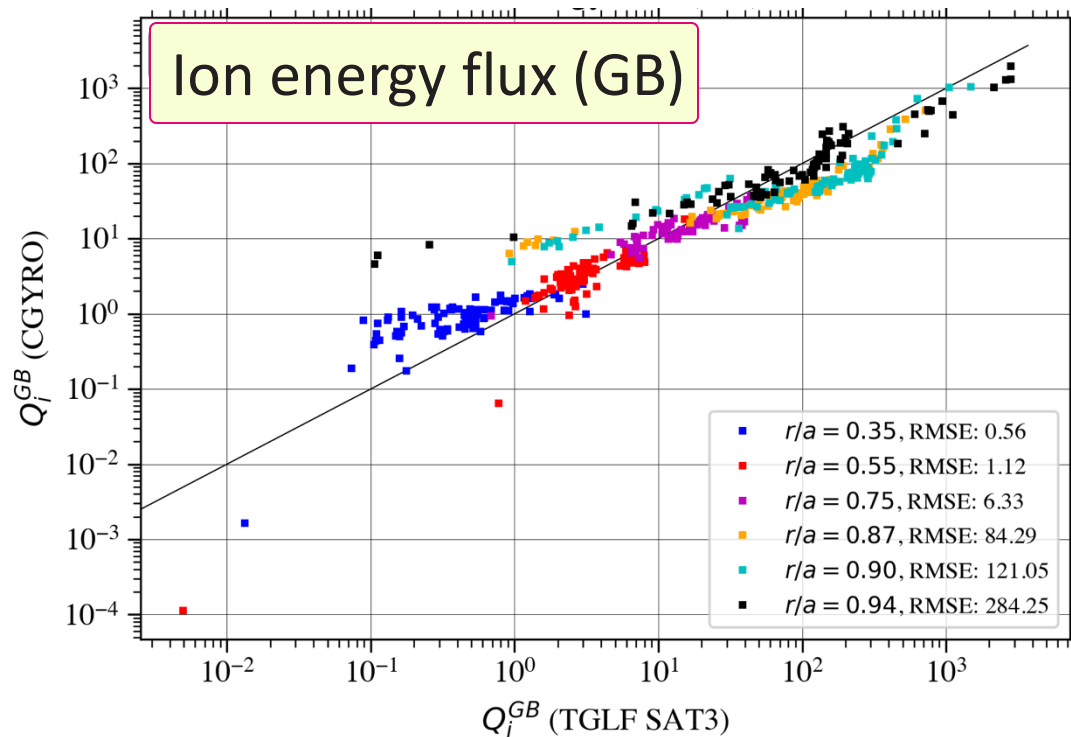


Consistent with experiment
(e.g. G. McKee PRL 2000)



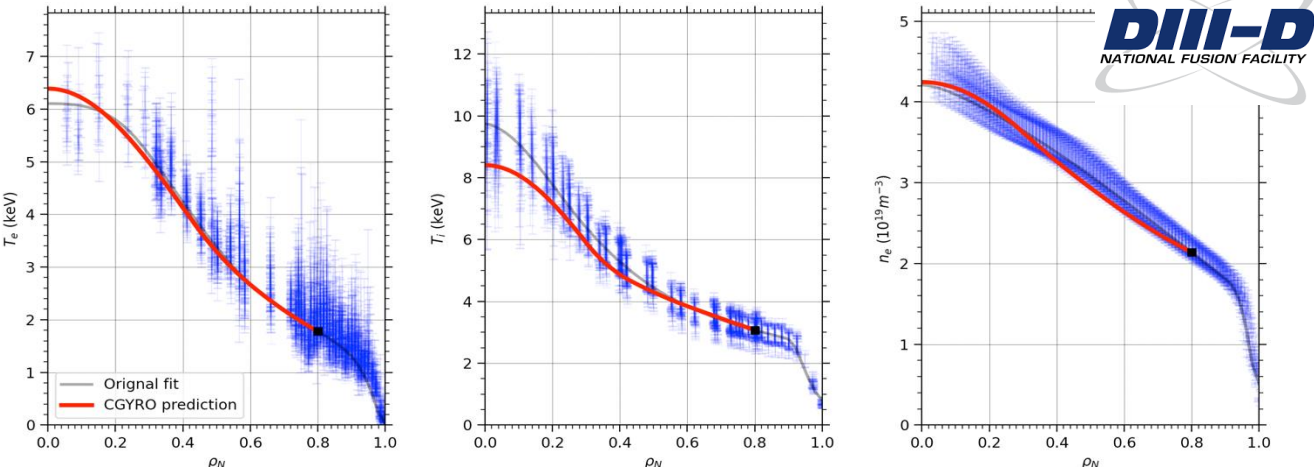
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- Exciting result: TGLF-SAT3 provides a reasonable proxy for core turbulence in these regimes.



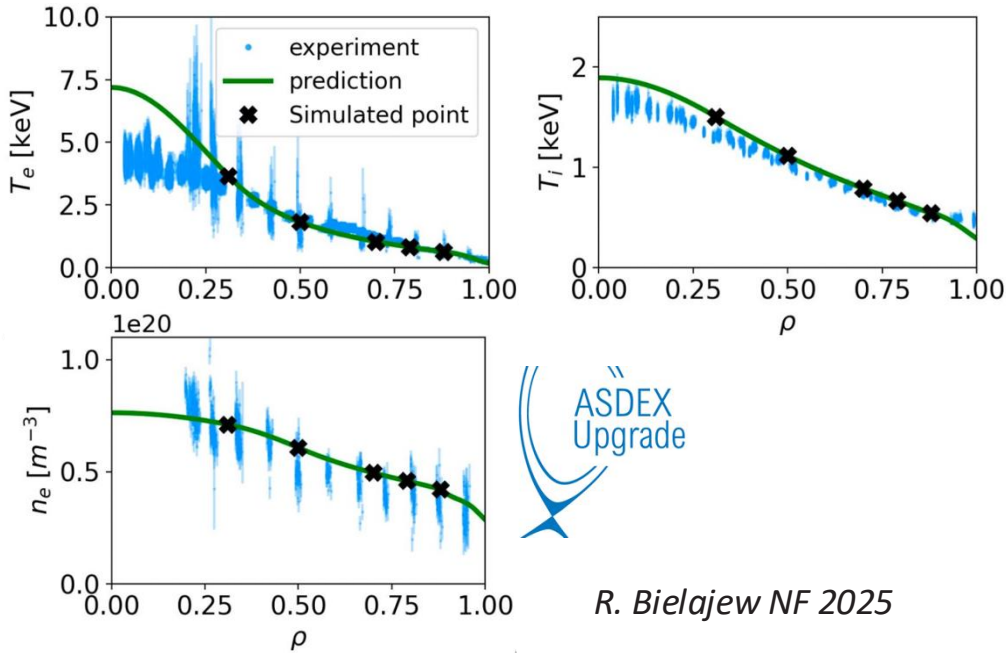
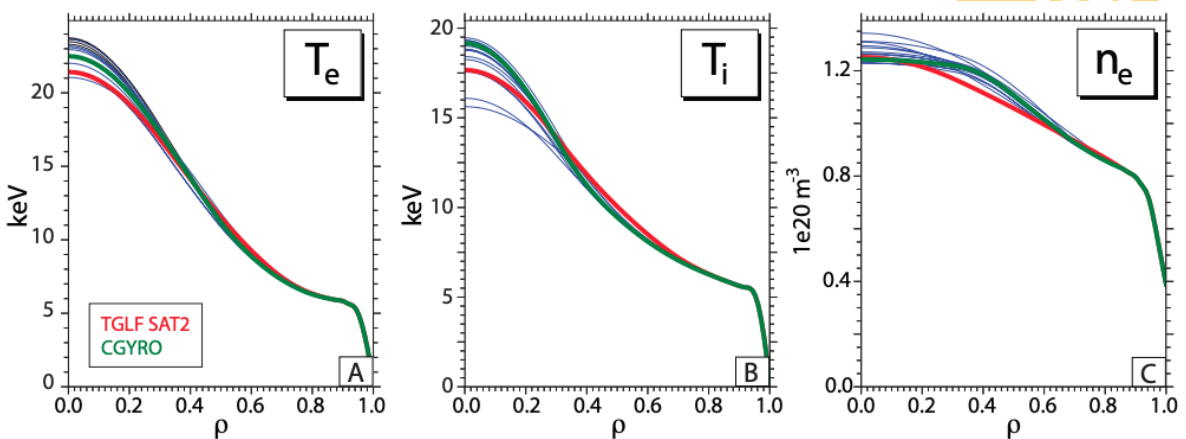
PORTALS-CGYRO is being used to study DIII-D, AUG, JET, ITER, ARC

N.T. Howard PoP 2024, P. Rodriguez-Fernandez NF 2024



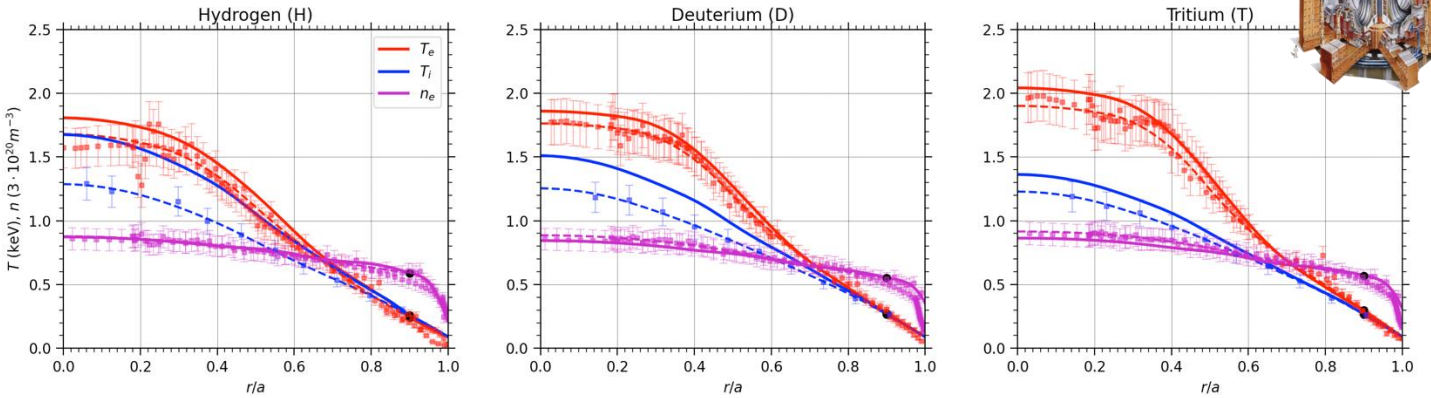
Over 50 PORTALS-CGYRO profile predictions so far

N.T. Howard NF 2025



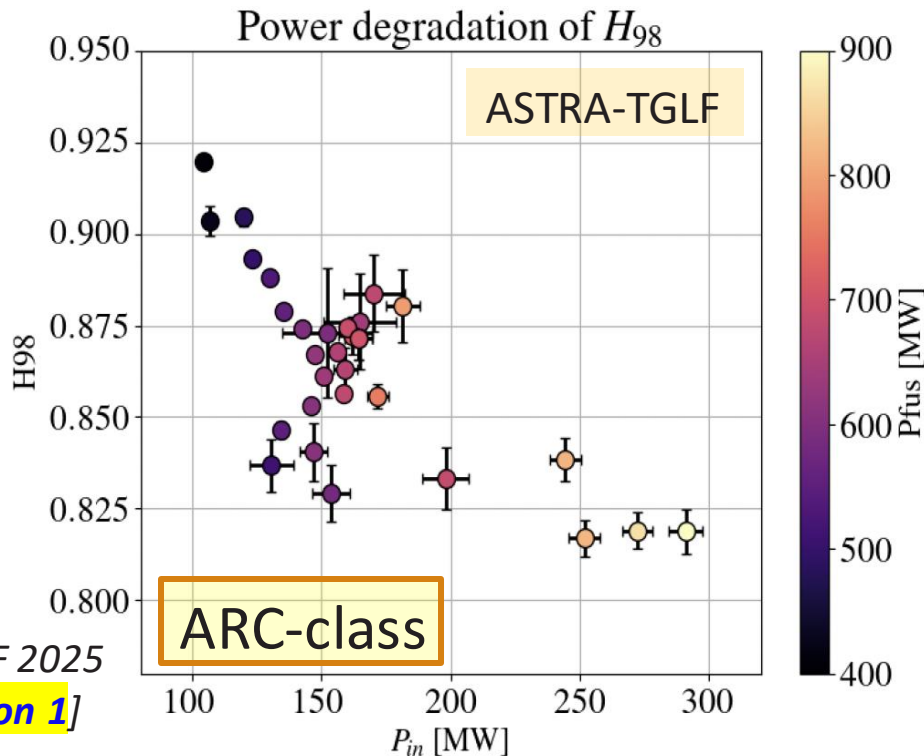
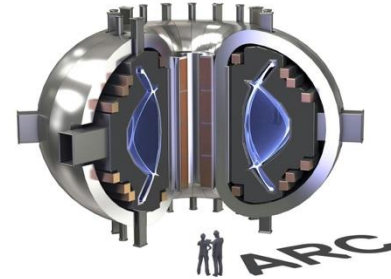
R. Bielajew NF 2025

P. Rodriguez-Fernandez EPS 2023

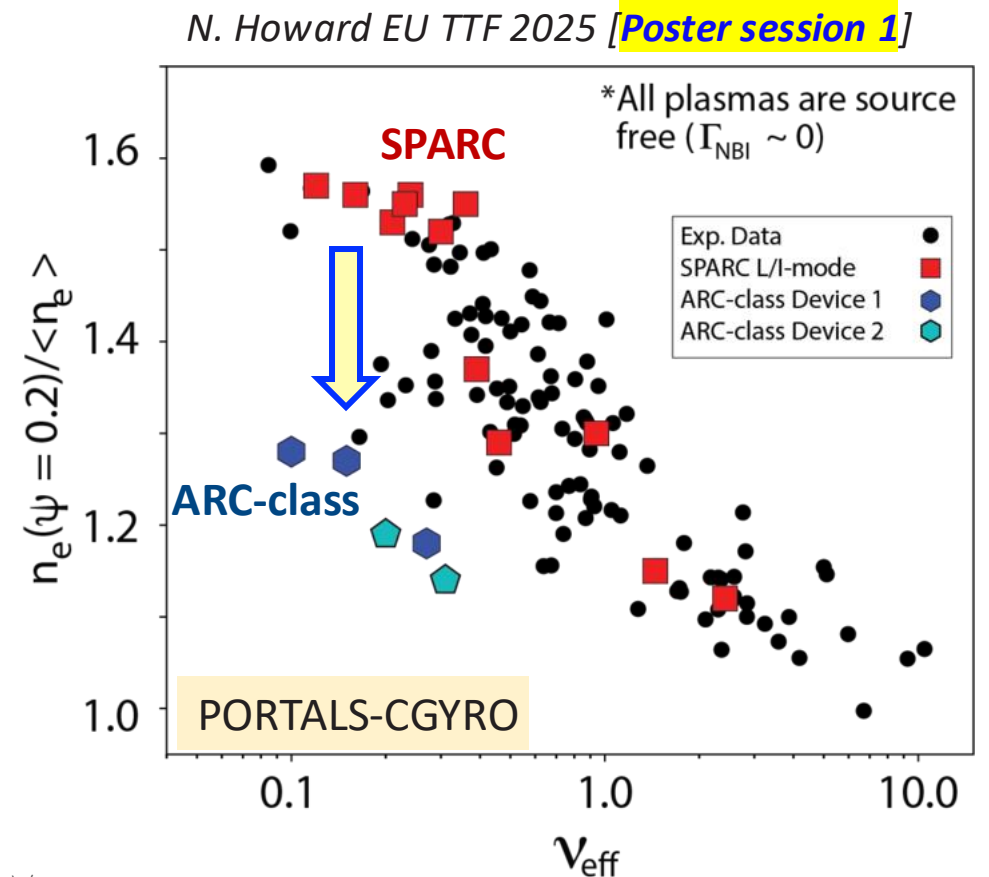


Physics-based modeling is becoming a key element to design ARC's core

- Turbulence and integrated modeling currently being used, in iteration with engineering teams and edge modelers, to design **ARC power plant's core**.
- Simulations point towards lower **density peaking** than expected from empirical scaling laws, and **stiff transport conditions** limit ability to raise volume-average temperature arbitrarily
- Key to account for physics-based modeling early on!



J. Hall EU TTF 2025
[Poster session 1]



- **Surrogate-optimization** in flux-matching problem of δf codes as embedded in PORTALS opens new pathways to:
 - 1) allow predictions of performance in future reactors, and
 - 2) study turbulence and validation in current experiments with first-principles simulations.
- **Physics-based integrated modeling** and **NL GK** are being used to plan SPARC campaigns and inform fusion power plant design to reduce risk of extrapolating from limited empirical databases.
- Profile predictions with NL GK especially useful when **quasilinear models not fully developed or validated** (e.g. *spherical, stellarators, fast ions*) and when they encounter difficulties (e.g. *source-free particle transport*).

PORTALS developments currently occurring under SciDAC-5 partnership

SMARTS: “Surrogate Models for Accurate and Rapid Transport Solutions”

GK databases, multi-fidelity, multi-channel, modularization and packaging

